

Compositional Verification of Concurrent Systems by Combining Bisimulations

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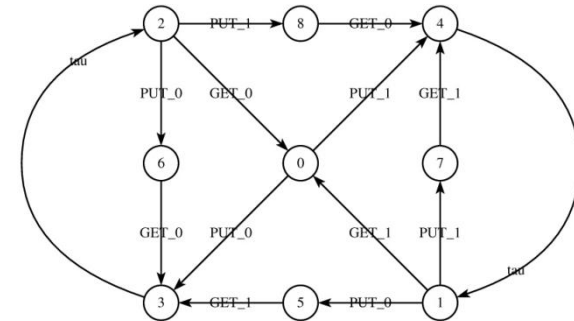
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Motivation

■ Explicit-state model checking of concurrent system

- ▶ Asynchronous model $P_1 || \dots || P_n$
- ▶ LTS (Labelled Transition System) semantics
- ▶ Action-based modal μ -calculus property φ



■ Problem: state-space explosion

■ Compositional verification can circumvent explosion

- ▶ Apply to $P_1 || \dots || P_n$ LTS reductions that preserve φ
- ▶ [Mateescu & Wijs \(2014\)](#) define φ -preserving reductions: action hiding and quotient wrt. strong **or** divbranching bisimulation
- ▶ Applied successfully to many case studies

■ We refine the approach by combining both bisimulations

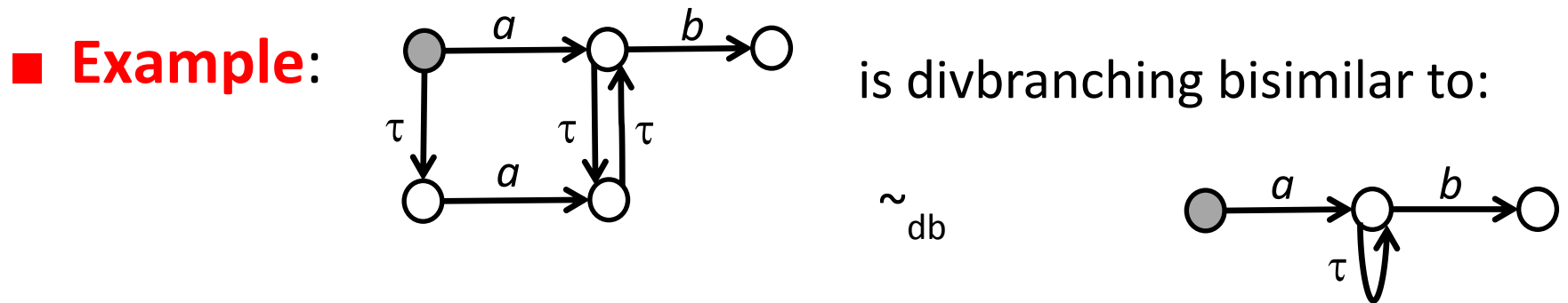
Outline

1. Background
2. The mono-bisimulation approach of **Mateescu & Wijs**
3. Our refined approach combining bisimulations
4. Applications and experimental results
5. Conclusion

1. Background

Divbranching bisimulation (van Glabbeek & Weijland, 1996)

- Short for **divergence-preserving branching bisimulation**
- Weaker than strong bisimulation:
special treatment of invisible (τ) transitions
- Preserves choices of visible actions and infinite sequences of τ -transitions



- Like strong, divbranching is a congruence for \parallel
 \Rightarrow reduction applicable compositionally

Compositional reduction

- Alternation between n-ary compositions/reductions (rcomp_n), until all processes are aggregated
- Many strategies are possible
Example: $P_1 \parallel P_2 \parallel P_3$
 - ▶ $\text{rcomp}_3 (\text{rcomp}_1 (P_1), \text{rcomp}_1 (P_2), \text{rcomp}_1 (P_3)))$,
 - ▶ $\text{rcomp}_2 (\text{rcomp}_2 (\text{rcomp}_1 (P_1), \text{rcomp}_1 (P_2))), \text{rcomp}_1 (P_3))$, ...
- LTS constrain each others by synchronization
- Aim: maintain the “largest intermediate LTS size” small
- No optimal strategy available: heuristic is needed
- We use **smart reduction** (Crouzen & Lang, 2011)

The action-based modal mu-calculus L_μ (Kozen, 1983)

- Temporal logic interpreted over LTS

- Action formulas:

$$\alpha ::= a \mid \mathbf{false} \mid \neg\alpha \mid \alpha_1 \vee \alpha_2$$

Notation: $[[\alpha]]$ set of actions satisfying α

- State formulas:

$$\varphi ::= \mathbf{false} \mid \neg\varphi_0 \mid \langle\alpha\rangle\varphi_0 \mid \varphi_1 \vee \varphi_2 \mid \mu X. \varphi_0 \mid X$$

Notation: $P \models \varphi$ LTS P satisfies φ

- Derived operators: $\mathbf{true} \mid [\alpha]\varphi_0 \mid \varphi_1 \wedge \varphi_2 \mid \nu X. \varphi_0$

- Subsumes (action-based) CTL, ACTL, PDL, PDL- Δ , etc.

2. The mono-bisimulation approach of Mateescu & Wijs

The mono-bisimulation approach

- Find actions a_1, \dots, a_m and relation R among **divbranching** and **strong** bisimulations, such that φ can be verified on

R reduction of hide a_1, \dots, a_m in $P_1 || \dots || P_n$

instead of

$P_1 || \dots || P_n$

- Procedure $H(\varphi)$ computes the largest set a_1, \dots, a_m

$H(\varphi) = \bigcap h(\alpha) \quad h(\alpha) = \text{if } \tau \in [[\alpha]] \text{ then } [[\alpha]] \text{ else all but } [[\alpha]]$

Example: $H(\mu X. \langle a \rangle \text{ true} \vee \langle \text{true} \rangle X) = \text{all but } a$

- A fragment $L_{\mu\text{-db}}$ of L_{μ} is defined such that:

- ▶ R is **divbranching** if $\varphi \in L_{\mu\text{-db}}$
- ▶ R is **strong** otherwise (less reduction)

The fragment $L_{\mu\text{-db}}$

Strong modalities $\langle \alpha \rangle \varphi$ are replaced by weak modalities:

$\varphi ::= \mathbf{false} \mid \neg \varphi_0 \mid \varphi_1 \vee \varphi_2 \mid \mu X. \varphi_0 \mid X$

$\mid \langle (\varphi_1?. \alpha_\tau)^* \rangle \varphi_2$

there is a sequence of actions satisfying α_τ that traverses only states satisfying φ_1 and ends in a state satisfying φ_2

$\mid \langle (\varphi_1?. \alpha_\tau)^*. \varphi_1?. \alpha_a \rangle \varphi_2$

there is a sequence of actions satisfying α_τ that traverses only states satisfying φ_1 and ends in a state satisfying $\langle \alpha_a \rangle \varphi_2$

$\mid \langle \varphi_1?. \alpha_\tau \rangle @$

there is an infinite sequence of actions satisfying α_τ that traverses only states satisfying φ_1

where $\tau \in [[\alpha_\tau]]$, $\tau \notin [[\alpha_a]]$

Expressiveness of $L_{\mu\text{-db}}$

Translation to $L_{\mu\text{-db}}$ is possible for the following operators:

- PDL- Δ : $\langle \alpha_\tau^* \rangle \varphi_0$ $\langle \alpha_\tau^* . \alpha_a \rangle \varphi$ $\langle \alpha_\tau \rangle @$
- ACTL: $\mathbf{A} (\varphi_1 \alpha_1 \mathbf{U} \varphi_2)$ $\mathbf{A} (\varphi_1 \alpha_1 \mathbf{U}_{\alpha_2} \varphi_2)$ $\mathbf{AG}_{\alpha_0} (\varphi_0)$
 $\mathbf{E} (\varphi_1 \alpha_1 \mathbf{U} \varphi_2)$ $\mathbf{E} (\varphi_1 \alpha_1 \mathbf{U}_{\alpha_2} \varphi_2)$ $\mathbf{EF}_{\alpha_0} (\varphi_0)$

($\mu\text{-ACTL}\setminus X$ is slightly less expressive than $L_{\mu\text{-db}}$)

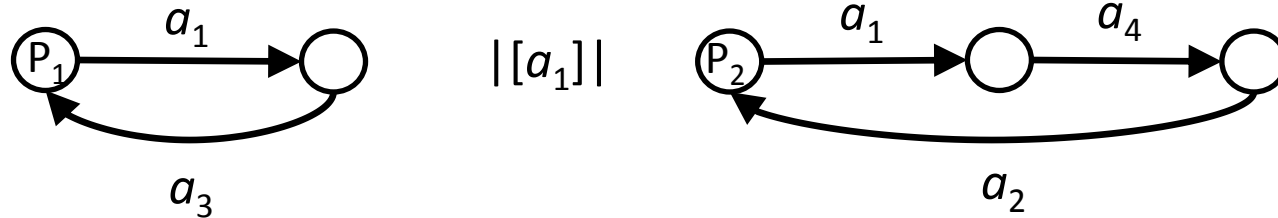
- CTL: $\mathbf{A} (\varphi_1 \mathbf{U} \varphi_2)$ $\mathbf{A} (\varphi_1 \mathbf{W} \varphi_2)$ $\mathbf{AG} (\varphi_0)$ $\mathbf{AF} (\varphi_0)$
 $\mathbf{E} (\varphi_1 \mathbf{U} \varphi_2)$ $\mathbf{E} (\varphi_1 \mathbf{W} \varphi_2)$ $\mathbf{EF} (\varphi_0)$ $\mathbf{EG} (\varphi_0)$

$\mathbf{A} (([\alpha_a] \varphi_1) \mathbf{U} \varphi_2)$	$\mathbf{A} (([\alpha_a] \varphi_1) \mathbf{W} \varphi_2)$
$\mathbf{AG} (\varphi_1 \vee [\alpha_a] \varphi_2)$	$\mathbf{EF} (\varphi_1 \wedge \langle \alpha_a \rangle \varphi_2)$

New result

where $\varphi_0, \varphi_1, \varphi_2 \in L_{\mu\text{-db}}, \tau \in [[\alpha_\tau]], \tau \notin [[\alpha_a]]$

Compositional verification example



- $\varphi_1 = \langle \text{true}^* . a_1 \rangle \text{true} \in L_{\mu\text{-db}}$
 smart divbranching reduction of
 hide all but a_1 in $(P_1 |[a_1]| P_2) \models \varphi_1$
 \Rightarrow Largest LTS: **3 states / 3 transitions** (P_2)

- $\varphi_2 = [\text{true}^* . a_1 . a_2] \text{false} \notin L_{\mu\text{-db}}$
 smart strong reduction of
 hide all but a_1, a_2 in $(P_1 |[a_1]| P_2) \models \varphi_2$
 \Rightarrow Largest LTS: **6 states / 8 transitions**

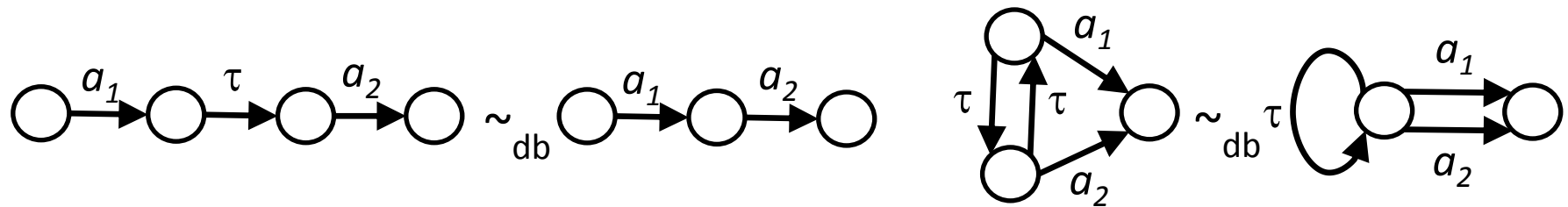
3. Our refined approach combining bisimulations

Principles

- Formulas may combine strong and weak modalities

Examples: $[\mathbf{true}^*.a_1.a_2]$ false $\langle \mathbf{true}^* \rangle (\langle a_1 \rangle \mathbf{true} \wedge \langle a_2 \rangle \mathbf{true})$

- Such formulas are not preserved by divbranching



- Theorem: If no action of some P_i is matched by a strong modality then P_i can be reduced for divbranching

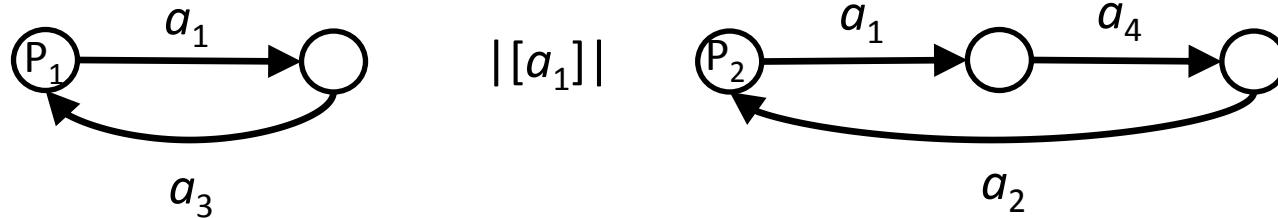
- We write $\varphi \in L_{\mu\text{-str}}(A_s)$ and call A_s the set of strong actions if all strong modalities of φ satisfy $[[\alpha]] \subseteq A_s$

Examples: $[\mathbf{true}^*.a_1.a_2]$ false $\in L_{\mu\text{-str}}(\{a_2\})$ $L_{\mu\text{-db}} = L_{\mu\text{-str}}(\emptyset)$

New verification strategy

- Partitioning the set of processes
 - ▶ \mathcal{P}_s : processes among P_1, \dots, P_n **containing strong actions**
 - ▶ $\mathcal{P}_w = \{P_1, \dots, P_n\} \setminus \mathcal{P}_s$: processes **not containing strong actions**
- Refactoring $P_1 || \dots || P_n$ into $(||_{P_s \in \mathcal{P}_s} P_s) || (||_{P_w \in \mathcal{P}_w} P_w)$
- Reducing the sets of processes compositionally according to theorem:
 - ▶ $Q =$ **smart divbranching reduction of** $(||_{P_w \in \mathcal{P}_w} P_w)$
 - ▶ $Q' =$ **smart strong reduction of** $(||_{P_s \in \mathcal{P}_s} P_s) || Q$
- Finally checking **hide** $H(\varphi)$ **in** $Q' \models \varphi$

Example



- $\varphi_2 = [\text{true}^*.a_1.a_2] \text{ false} \in L_{\mu\text{-str}}(\{a_2\})$
smart strong reduction of hide all but a_1, a_2 in
((smart divbranching reduction of $-- a_2 \notin P_1$
hide all but a_1 in P_1)
 $|[a_1]|$
(smart strong reduction of $-- a_2 \in P_2$
hide all but a_1, a_2 in P_2)) $\models \varphi_2$
- \Rightarrow Largest LTS: **3 states / 3 transitions**
 instead of 6 states / 8 transitions

Extracting A_s from the formula

- **Problem:** Given $\varphi \in L_\mu$, how to infer A_s s.t. $\varphi \in L_{\mu\text{-str}}(A_s)$?
- Hard for arbitrary low-level L_μ formula
 - ▶ Need to prove that a strong modality can be turned to weak one
 - ▶ Analogy: prove that binary code implements function correctly
- Easier for higher-level logics (CTL, ACTL, PDL, PDL- Δ):
Use knowledge of $L_{\mu\text{-db}}$ expressiveness (patterns)
Example: $A (([a] \text{ false}) \mathbf{U} \langle b \rangle \text{ true}) \in L_{\mu\text{-str}}(\{b\})$
because $A (([\alpha_a] \varphi_1) \mathbf{U} \varphi_2) \in L_{\mu\text{-db}}$ and $\langle b \rangle \text{ true} \in L_{\mu\text{-str}}(\{b\})$
- A_s can be safely over-approximated, but smaller is better
- Automatic extraction of minimal A_s faces issues

Issues with extracting a minimal A_s

■ Issue 1: It requires semantic reasoning

- ▶ **Example:** in $\mathbf{AG} (\langle a \rangle \mathbf{true} \Rightarrow [a] \varphi_0)$, a seems to be strong
In fact it is not as this formula is equivalent to $\mathbf{AG} ([a] \varphi_0)$
- ▶ L_μ satisfiability checking (EXPTIME) might be necessary

■ Issue 2: minimal A_s is not unique

- ▶ **Example:** $\varphi = \langle \mathbf{true}^* \rangle (\langle a_1 \rangle \mathbf{true} \wedge \langle a_2 \rangle \mathbf{true}) \notin L_{\mu\text{-str}}(\emptyset)$
 $\varphi \equiv \langle (\langle a_1 \rangle \mathbf{true}?.\mathbf{true})^* . \langle a_1 \rangle \mathbf{true}?.a_2 \rangle \mathbf{true} \in L_{\mu\text{-str}}(\{a_1\})$
 $\varphi \equiv \langle (\langle a_2 \rangle \mathbf{true}?.\mathbf{true})^* . \langle a_2 \rangle \mathbf{true}?.a_1 \rangle \mathbf{true} \in L_{\mu\text{-str}}(\{a_2\})$
- ▶ a_1 and a_2 can be weak actions but not both simultaneously
- ▶ Choosing one or the other may impact performance

■ In general: rely on expertise, side proof needed

4. Applications and experimental results

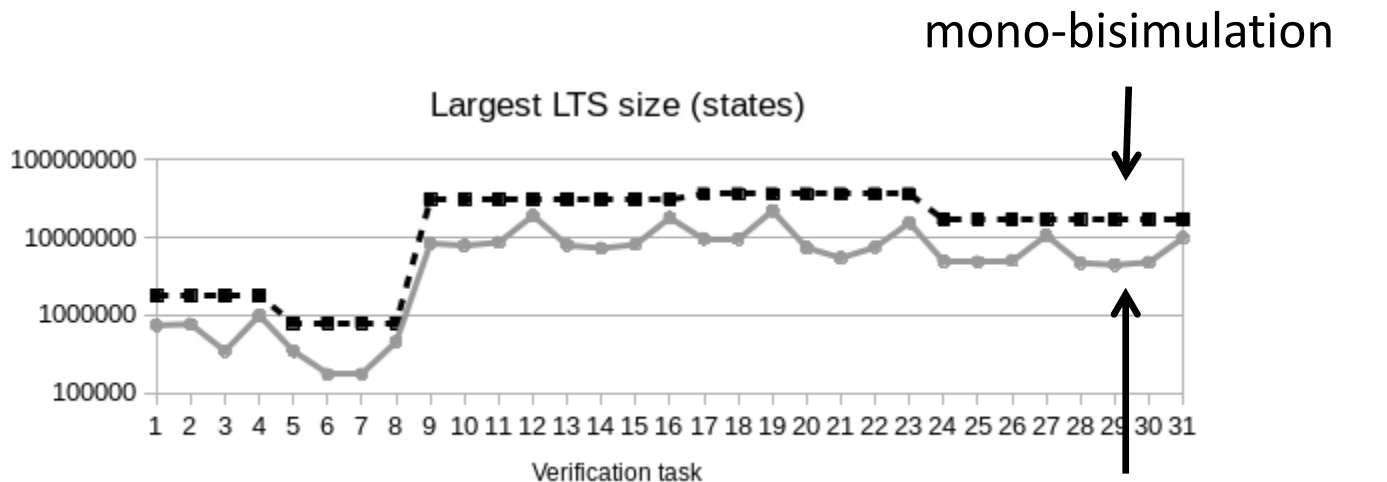
Implementation



- Approach implemented using **CADP** toolbox (cadp.inria.fr)
 - ▶ Formal verification of asynchronous concurrent systems
 - ▶ Toolbox developed since the late 80's (≈ 70 tools and libraries)
- Several software components used in this work:
 - ▶ **LNT.OPEN/GENERATOR**: compiling LNT processes to LTS
 - ▶ **EXP.OPEN 2/GENERATOR**: composing LTS in parallel
 - ▶ **BCG_MIN 2**: minimizing LTS for strong and divbranching
 - ▶ **BCG_OPEN/EVALUATOR 4**: model checking MCL temporal logic (regular alternation-free modal mu-calculus with data)
 - ▶ **SVL**: scripting, smart compositional verification heuristic
- Successful application to several examples

TFTP (Trivial File Transfer Protocol)

- Avionics case study (Garavel&Thivolle, 2009)
- 31 verification tasks involve properties that contain both weak and strong modalities
- Comparison with the mono-bisimulation approach
- Result: largest LTS up to **7 times smaller**



Gains in CPU time and memory peak are similar

combined bisimulations

RERS (Rigorous Evaluation of Reactive Systems)

- Verification competition <http://rers-challenge.org>
- RERS 2018 “parallel CTL” benchmark
 - ▶ 3 concurrent models (101...103) with 9 to 34 parallel processes
 - ▶ 9 properties – 3 per model (21..23)
- 7 properties combine weak and strong modalities
- Mono-bisimulation: explosion for 5 properties
- Combined bisimulations approach is successful
 - ▶ 4 properties from 5 to 10 min. and from 22 to 101 MB
 - ▶ 1 property: 42 min. and 1.6 GB

RERS - CTL example (103#23)

- **AG** ($\langle A34 \rangle$ **true** \Rightarrow $[A34]$ **A** ($[A68]$ **false** $W \langle A59 \rangle$ **true**))
checked on a composition of **34 processes** (**70 actions**)
 - ▶ All but **A34** , **A59** , **A68** can be hidden (67 actions)
 - ▶ **A34** , **A68** are weak, formula belongs to $L_{\mu\text{-str}}(\{A59\})$
- Mono-bisimulation (strong) does not prevent explosion
 - ▶ Stopped after several hours
 - ▶ Largest LTS: \geq **4.5 Giga states / 36 Giga transitions**
- Combining bisimulations is successful
 - ▶ Strong action in 7 proc. \Rightarrow 27 proc. reduced for divbranching
 - ▶ Result **true** after $<$ **10 min CPU**, using **35 MB** memory
 - ▶ Largest LTS: **122,292 states / 888,156 transitions**



5. Conclusion

- Improvement of property-preserving LTS reductions
 - ▶ New strategy combining bisimulations applicable to properties not preserved by divbranching bisimulation
 - ▶ Based on property analysis, classifying actions as weak or strong
 - ▶ Big LTS reductions wrt. mono-bisimulation
 - ▶ Proofs and examples available at doi.org/10.5281/zenodo.2634148
- Future work:
 - ▶ Automate A_s computation or automatically check user-given A_s
 - ▶ Automate composition refactoring $(\parallel_{P_s \in \mathcal{P}_s} P_s) \parallel (\parallel_{P_w \in \mathcal{P}_w} P_w)$
 - ▶ Approach further refined \Rightarrow gold medals won at RERS 2019