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# Translating Pi-Calculus into LOTOS NT

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# Introduction

- We present here a novel **translation** from **pi-calculus** to a classical process algebra, namely LOTOS NT
- We focus here on the **finite control fragment** of the pi-calculus
- LOTOS NT being an input language of the CADP toolbox, our approach allows to **verify pi-calculus specifications** using all the state-of-the-art verification tools available in CADP
- Our translation is **fully automated** by the pic2Int prototype tool

# Outline

- Pi-Calculus and LOTOS NT
- Translation
- Prototype Tool
- Case Study: A Dispatcher Service
- Concluding Remarks

# Pi-calculus

- We consider the original version of Pi-calculus equipped with the **early** operational semantics
- For the sake of simplicity, we focus on the **monadic** Pi-calculus, but our translator accepts a polyadic Pi-calculus

- **Grammar** of Pi-calculus:

$$P ::= 0 \mid \tau.P \mid \underline{x}y.P \mid x(y).P \mid P_1 \mid P_2 \mid P_1 + P_2 \mid \\ (\nu x)P \mid [x=y]P \mid [x \neq y]P \mid A(x_1, \dots, x_r)$$

- Agents do **not contain recursive calls** through the parallel composition operator (finite control property)

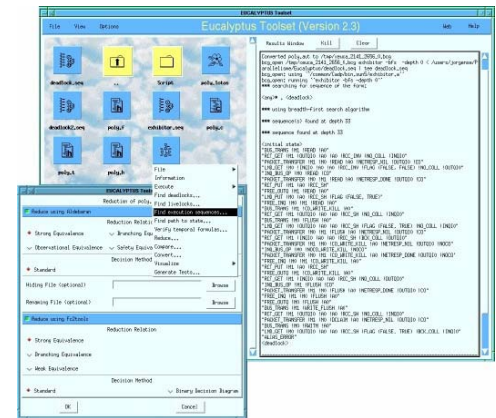
# LOTOS NT

- LOTOS NT is a **value-passing process algebra** with user-friendly syntax and operational semantics
- The specification language consists of two parts:
  - A **functional language** to describe data types
  - An **imperative-like** formalism to specify processes
- Grammar of the behavioural **LOTOS NT fragment** we use:  
$$\begin{array}{l} B ::= \text{stop} \mid G(!E, ?X) \text{ where } E' \mid \text{if } E \text{ then } B \text{ end if} \\ \mid \text{var } x:T \text{ in } x:=E ; B \text{ end var} \mid \text{hide } G \text{ in } B \text{ end hide} \\ \mid P [G_1, \dots, G_m] (E_1, \dots, E_n) \mid \text{select } B_1 [] \dots [] B_n \text{ end select} \\ \mid \text{par } G \text{ in } B_1 \parallel \dots \parallel B_n \text{ end par} \end{array}$$
- Verification using CADP through a **translation to LOTOS**

# Construction and Analysis of Distributed Processes (CADP)

## ➤ Design of **asynchronous systems**

- Concurrent processes
- Message-passing communication
- Nondeterminism



## ➤ **Formal approach** rooted in concurrency theory: process calculi, Labeled Transition Systems, temporal logics

## ➤ Many **verification techniques**: simulation, model and equivalence-checking, compositional verification, test case generation, performance evaluation, etc

## ➤ Numerous **practical applications**, *e.g.*, telecommunications, middleware and software architectures, hardware

# Pi-calculus versus LOTOS NT

## Differences

Binary rendez-vous	Multi-way rendez-vous
Unidirectional communication	Bidirectional communication
Mobile channels	Static channels
Dynamic creation of processes	Static network of processes
Names only	Constructed datatypes
Action prefix	Symmetric sequential compo.

## Similarities

Choice, recursion

Binary parallel composition

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## Channel Names (1/2)

- Two classes of channels, **public** ( $G_{\text{pub}}$ ) and **private** ( $G_{\text{priv}}$ ), used to model **non-synchronized communications**
- We cannot use LOTOS NT static gates to represent mobile communication
- We represent Pi-calculus channel names as **values** of a LOTOS NT **datatype Chan**
- We model channel mobility between Pi-calculus agents by **communicating values** of this type along gates

## Channel Names (2/2)

The following type Chan is generated for  $(\nu x)(\underline{a}b.\underline{c}x.0)$

```
type Chan is
```

```
  a, b, c, x(id:Nat) with "==" , "!="
```

```
end type
```

```
function new_id () : Nat is
```

```
  !external null
```

```
end function
```

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```
function is_public (ch:Chan) : Bool is
```

```
  case ch in
```

```
    a|b|c → return true
```

```
    | any → return false
```

```
  end case
```

```
end type
```

# Action Prefix (1/2)

- The translation takes as input:
  - A Pi-calculus agent  $P$ ,
  - The gates  $\underline{G}$  on which  $P$  communicates with its environment, and
  - A natural  $k$  (pid) identifying the concurrent activity
- Communication on a channel  $x$  is translated using a **choice on all gates  $\underline{G}$**  connecting the term  $P$  to its environment
- Binary unidirectional communications are encoded using **different gate names** (one for each  $|$ ) and identifying explicitly the **sender and receiver** using placeholders

# Action Prefix (2/2)

```
t(xy.P, {G1, ..., Gn, Gpub, Gpriv}, k) =  
  select var r: Nat in  
    G1 (!x, !y, !k, ?r) [] ... [] Gn (!x, !y, !k, ?r) []  
    Gpub (!x, !y, !true) where is_public(x) []  
    Gpriv (!x, !y, !true) where not(is_public(x))  
  end select; t(P, {G1, ..., Gn, Gpub, Gpriv}, k)
```

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```
t(x(y).P, {G1, ..., Gn, Gpub, Gpriv}, k) =  
  select var s: Nat, y: Chan in  
    G1 (!x, ?y, ?s, !k) [] ... [] Gn (!x, ?y, ?s, !k) []  
    Gpub (!x, ?y, !false) where is_public(x) []  
    Gpriv (!x, ?y, !false) where not(is_public(x))  
  end select; t(P, {G1, ..., Gn, Gpub, Gpriv}, k)
```

# Sum, Match, Mismatch, Parallel, Channel Creation

$$t(P_1 + P_2, \underline{G}, k) = \text{select } t(P_1, \underline{G}, k) [] t(P_2, \underline{G}, k) \text{ end select}$$

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$$t([x=y]P, \underline{G}, k) = \text{if } x=y \text{ then } t(P, \underline{G}, k) \text{ end if}$$
$$t([x \neq y]P, \underline{G}, k) = \text{if } x \neq y \text{ then } t(P, \underline{G}, k) \text{ end if}$$

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$$t(P_1 | P_2, \underline{G}, k) = \text{hide } G_{\text{new}} \text{ in par } G_{\text{new}} \text{ in}$$
$$t(P_1, \underline{G} \cup \{G_{\text{new}}\}, 2k) || t(P_2, \underline{G} \cup \{G_{\text{new}}\}, 2k+1)$$
$$\text{end par end hide}$$

---

$$t((\nu x)P, \underline{G}, k) = \text{var } x:\text{Chan in } x := x(\text{new\_id}()); t(P, \underline{G}, k) \text{ end var}$$

# Agent Definition / Instantiation, Main Specification

$t(A(x_1, \dots, x_r) = P, \underline{G}, k) = \text{process } A_d [\underline{G}] (x_1, \dots, x_r : \text{Chan}, k : \text{Nat}) \text{ is}$   
 $t(P, \underline{G}, k)$   
 $\text{end process}$

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$t(A(y_1, \dots, y_r), \underline{G}, k) = A_d [\underline{G}] (y_1, \dots, y_r, k)$

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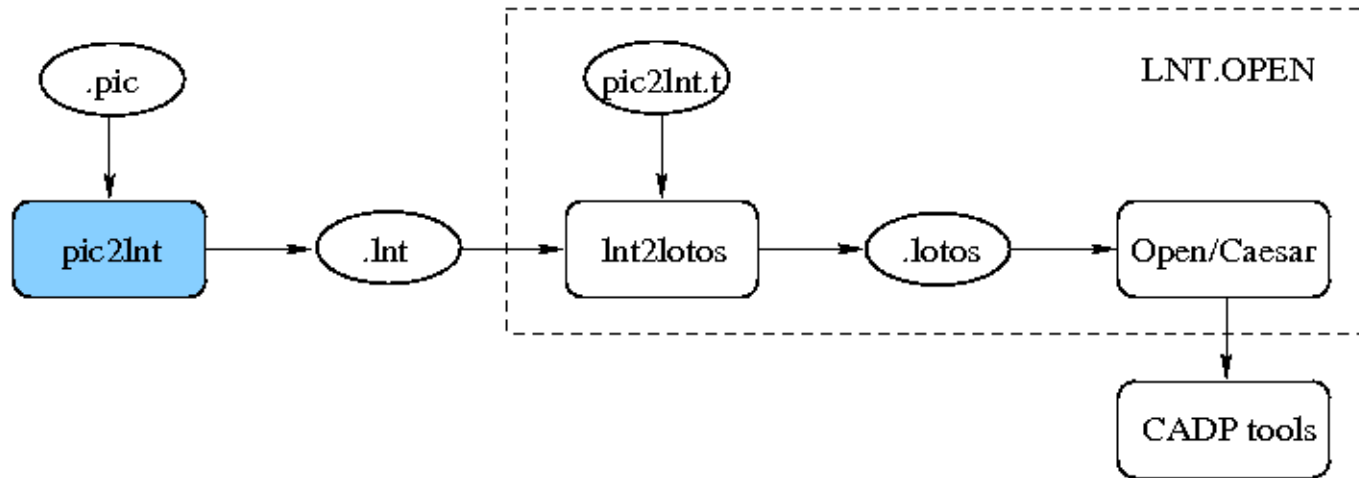
$\text{pic2Int}(P) = \text{par } G_{\text{priv}} \text{ in } t(P, \{G_{\text{pub}}, G_{\text{priv}}\}, 1) \text{ || stop end par}$

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- **Prototype Tool**
- Case Study: A Dispatcher Service
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# Prototype Tool

- The translation is **completely automated** by a tool we implemented



- Our benchmark currently contains **160 files**:  
2000 lines of Pi-calculus → 23000 lines of LOTOS NT



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# A Dispatcher Service in Pi-Calculus

Main = (nu req, a, b, c)

( Client(req,a,b,c) | Dispatcher(req) | Server(a) | Server(b) | Server(c) )

Client (req,a,b,c) = (nu x) ( request a.req<a,x>.ClientAux(req,a,a,b,c,x) ) +  
(nu x) ( request b.req<b,x>.ClientAux(req,b,a,b,c,x) ) +  
(nu x) ( request c.req<c,x>.ClientAux(req,c,a,b,c,x) )

ClientAux(req,k,a,b,c,x) =

x(info).( x purchase.purchase k.0 + x refuse.refuse k.Client(req,a,b,c) )

Dispatcher(req) = req(k,x).k x.Dispatcher(req)

Server(k) = k(x).x info.x(decision).Server(k)

# Dispatcher Service in LOTOS NT (1/2)

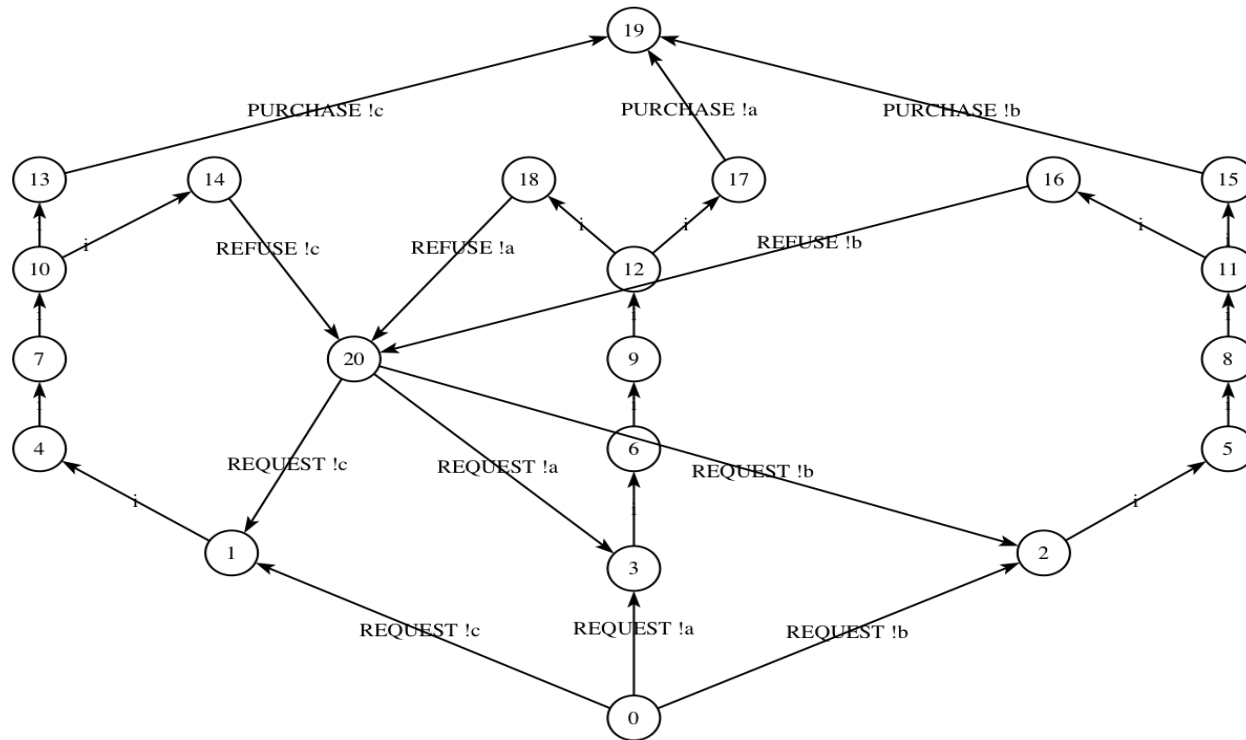
```
process MAIN [PUBLIC,PRIVATE:any] is
  var req, a, b, c:Chan in
    req:=req(new_id()); a:=a(new_id()); b:=b(new_id()); c:=c(new_id());

    hide G0:any in par G0 in hide G1:any in par G1 in
      hide G2:any in par G2 in hide G3:any in par G3 in
        Client_4 [PUBLIC,PRIVATE,G0,G1,G2,G3] (req,a,b,c,2)
        || Dispatcher_4 [PUBLIC,PRIVATE,G0,G1,G2,G3] (req,6)      end par end hide
        || Server_3 [PUBLIC,PRIVATE,G0,G1,G2] (a,14)              end par end hide
        || Server_2 [PUBLIC,PRIVATE,G0,G1] (b,30)                 end par end hide
        || Server_1 [PUBLIC,PRIVATE,G0] (c,31)                    end par end hide
      end var
    end process
```

# Dispatcher Service in LOTOS NT (2/2)

```
process Dispatcher_4 [PUBLIC,PRIVATE,G0,G1,G2,G3:any] (req:Chan,pid:Nat) is
  select var k,x:Chan, s:Nat in
    G0 (!req, ?k, ?x, ?s, !pid) [] G1 (!req, ?k, ?x, ?s, !pid) []
    G2 (!req, ?k, ?x, ?s, !pid) [] G3 (!req, ?k, ?x, ?s, !pid) []
    PUBLIC (!req, ?k, ?x, !false) where is_public(req) []
    PRIVATE (!req, ?k, ?x, !false) where not(is_public(req))
  end select ;
  select var r:Nat in
    G0 (!k, !x, !pid, ?r) [] G1 (!k, !x, !pid, ?r) []
    G2 (!k, !x, !pid, ?r) [] G3 (!k, !x, !pid, ?r) []
    PUBLIC (!k, !x, !true) where is_public(k) []
    PRIVATE (!k, !x, !true) where not(is_public(k))
  end select ; Dispatcher_4 [PUBLIC,PRIVATE,G0,G1,G2,G3] (req,pid)
end process
```

# LTS of the Dispatcher Service



One can use for instance the Evaluator model-checker to check MCL formulas, *e.g.*, "each request submitted by the client is eventually answered positively"

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# Concluding Remarks

- We have presented a **translation** from the finite fragment of the **Pi-calculus to LOTOS NT**
- This translation makes possible to **analyze Pi-calculus specifications** using the **CADP verification tools**
- The translation is **fully automated** by the pic2Int tool we implemented and validated on many examples
- Main perspective: extending the Pi-calculus with **data-handling features** to widen its possible application domains (applied Pi-calculus)