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# Hierarchical Adaptive State Space Caching Based on Level Sampling

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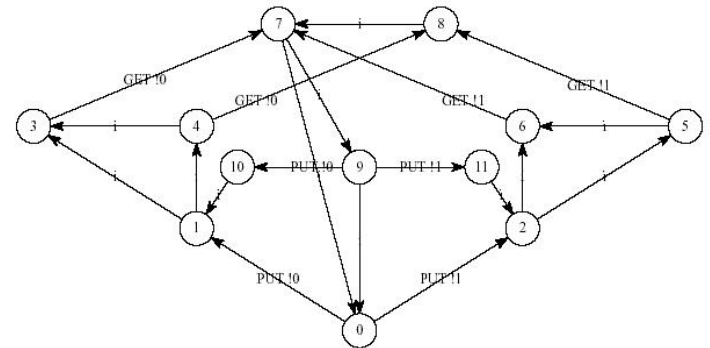
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- Labelled Transition System (LTS)/ Breadth-first Search (BFS)
- Partial Storage of Search History
- BFS With Snapshots
- BFS With Snapshot Caches
- Implementation
- Methods
- Conclusions & Future Work



# Labelled Transition System (LTS)

- LTS  $M=(S, A, T, s_0)$  with
  - $S$  a set of states
  - $A$  a set of transition labels
  - $T: S \times A \times S$  a transition relation
  - $s_0$  the initial state
- Framework: the CADP toolbox
  - <http://www.inrialpes.fr/vasy/cadp>



# Breadth-First Search

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## Algorithm 1 BFS

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```
procedure BFS( $s_0$ )  
   $Open \leftarrow \{s_0\}$  {Initial state added to horizon}  
   $Closed \leftarrow \emptyset$  {History is empty}  
  while  $Open \neq \emptyset$  do {Repeat until there are no more states to explore}  
    for all  $s \in Open$  do {Explore all states in the horizon}  
       $Next \leftarrow Next \cup \{s' \mid \exists \ell. (s, \ell, s') \in en(s)\}$   
       $Closed \leftarrow Closed \cup Open$  {Add explored states to history}  
       $Open \leftarrow Next \setminus Closed$  {Add new states to horizon}
```

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# Partial Storage of Search History

- State Space Explosion Problem
  - Linear growth of # concurrent processes -> exponential growth # states in LTS
- Memory problems due to having to store all states in history (*Closed*) in memory
- One approach is to consider partial storage -> research can be divided in two classes:
  - *Guaranteeing exhaustiveness*
  - Not guaranteeing exhaustiveness



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# Guarantee exhaustiveness

- Depth-first search (DFS) With Caching
  - Holzmann '87
  - Jard & Jéron '91
  - Godefroid et al. '95 add POR and static analysis
- Behrmann et al. 2003 use storing strategies involving static analysis
- From AI, e.g. *IDA\**, *MA\**; use structural info



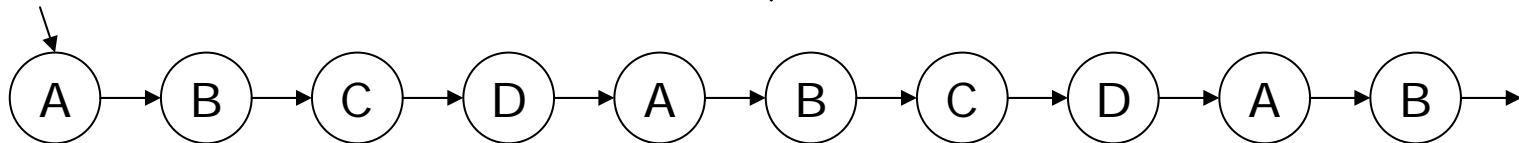
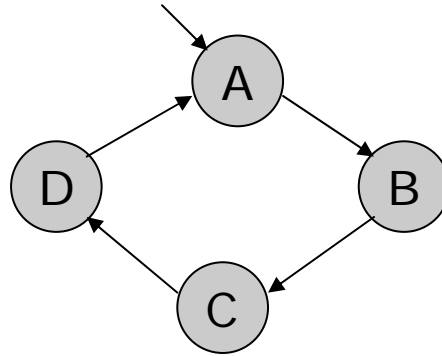
# Our Goals

- Other attempts concern reachability analysis, we want *state space generation*
- -> Besides dropping memory use, we also want LTSs with few redundancy
- Most concern DFS, we also want BFS
- Probabilistic <-> Certainty
  - Exhaustiveness
  - Termination
- We do *not* want static analysis (language independent)

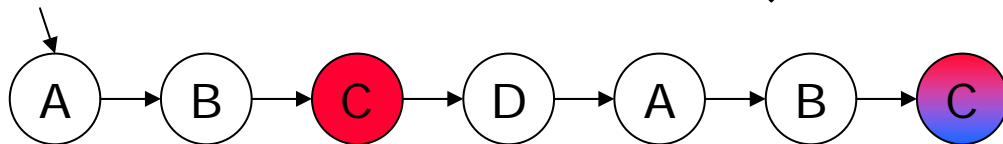
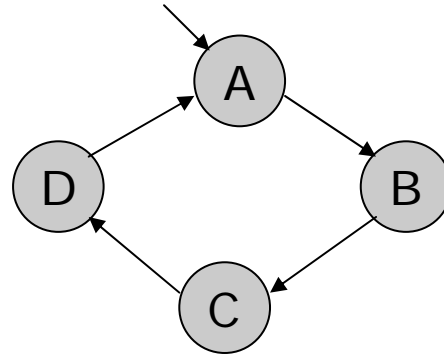




# No Duplicate Detection



# Partial Duplicate Detection



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# BFS With Snapshots

- State Space Explosion due to growth of *Closed* set
- Restricting growth will lead to partial failure of duplicate detection
- -> Result is LTS with redundancy

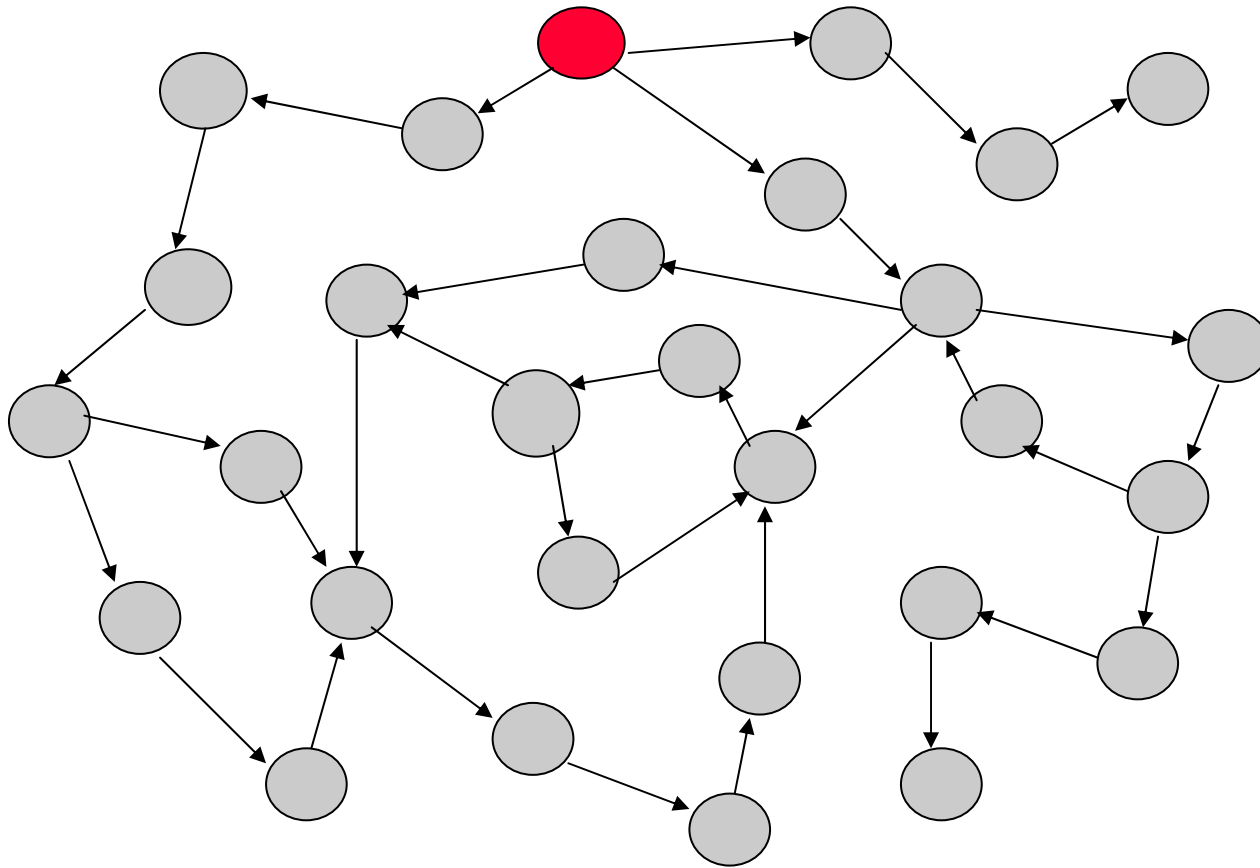


# What to Store?

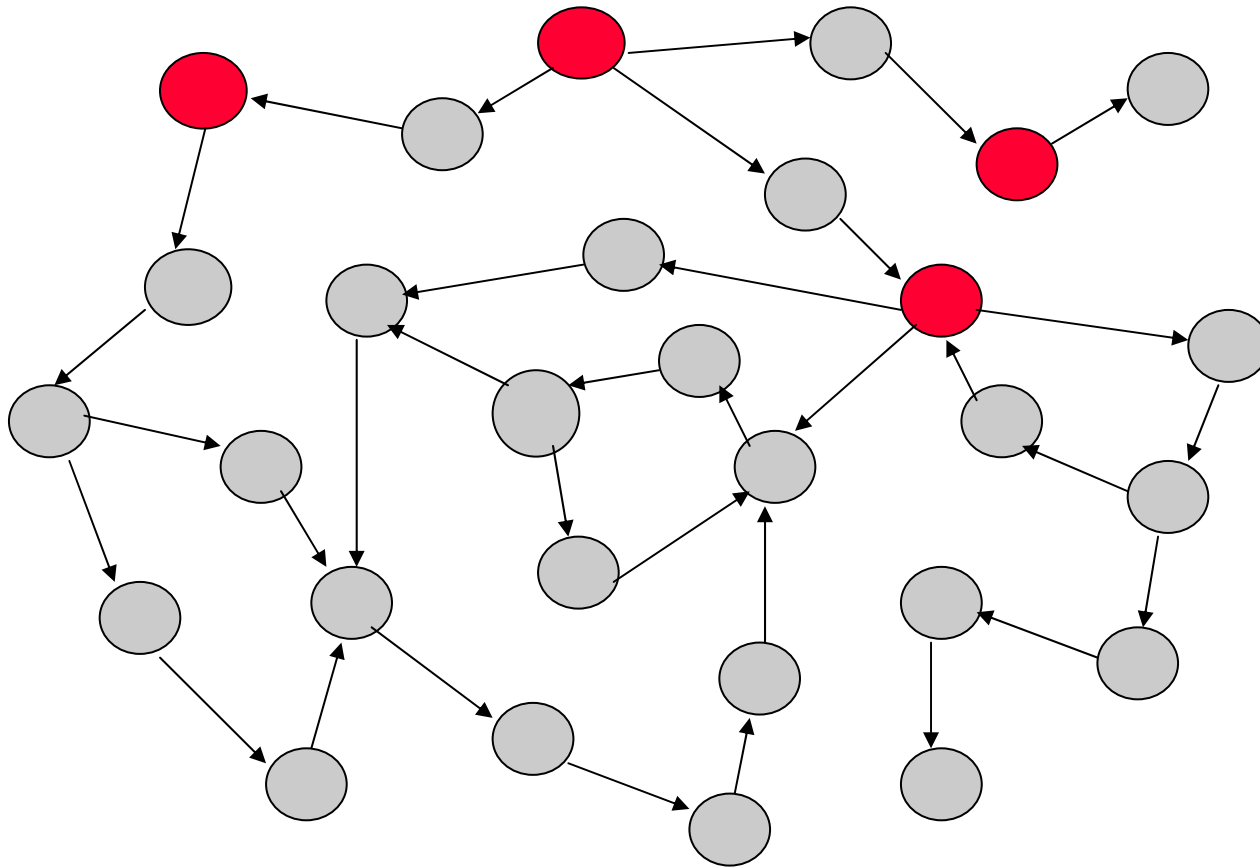
- No a priori knowledge structure LTS
  - Attempts at predicting exist; but theoretically, “anything can happen”
- Termination should be guaranteed
- -> We sample levels as *snapshots*
- Levels should be stored completely, otherwise states may “slip through”



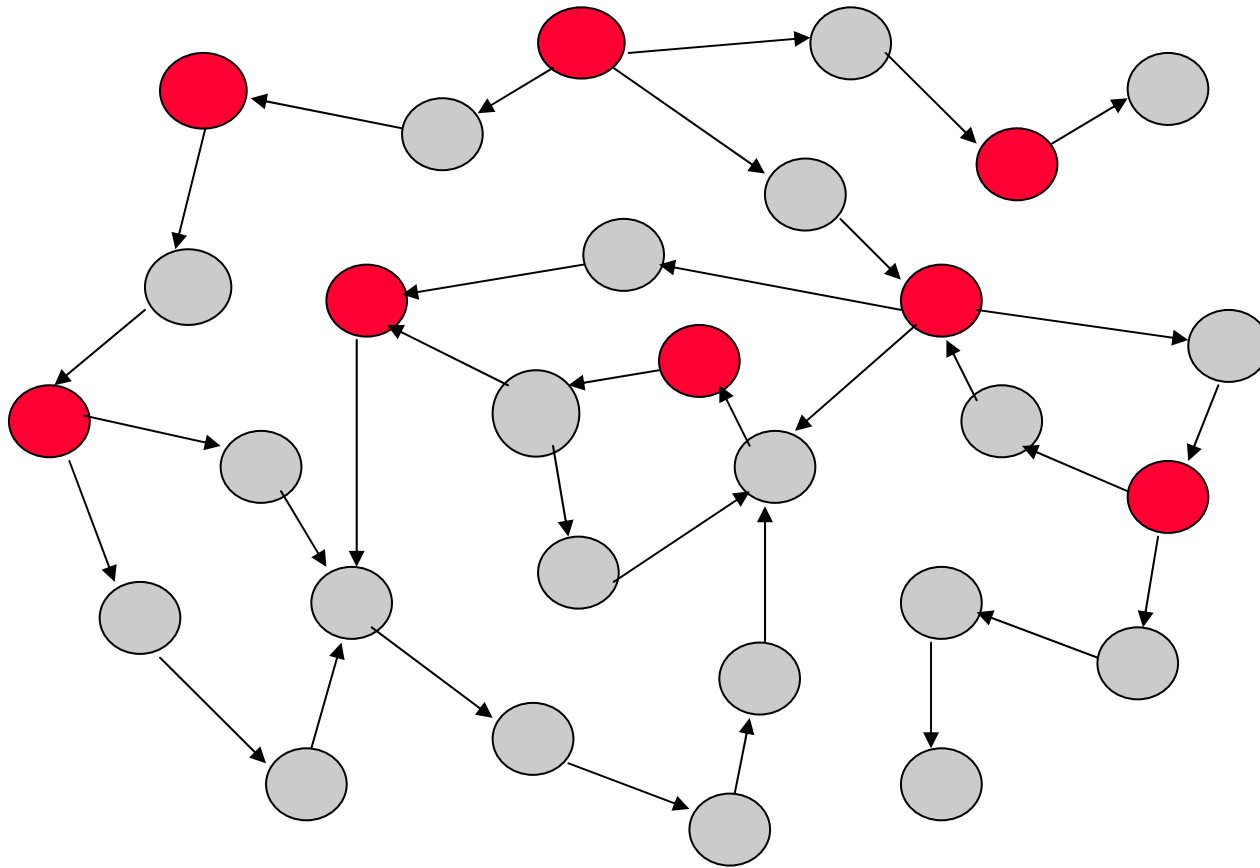
# BFS With Snapshots (period=2)



# BFS With Snapshots (period=2)

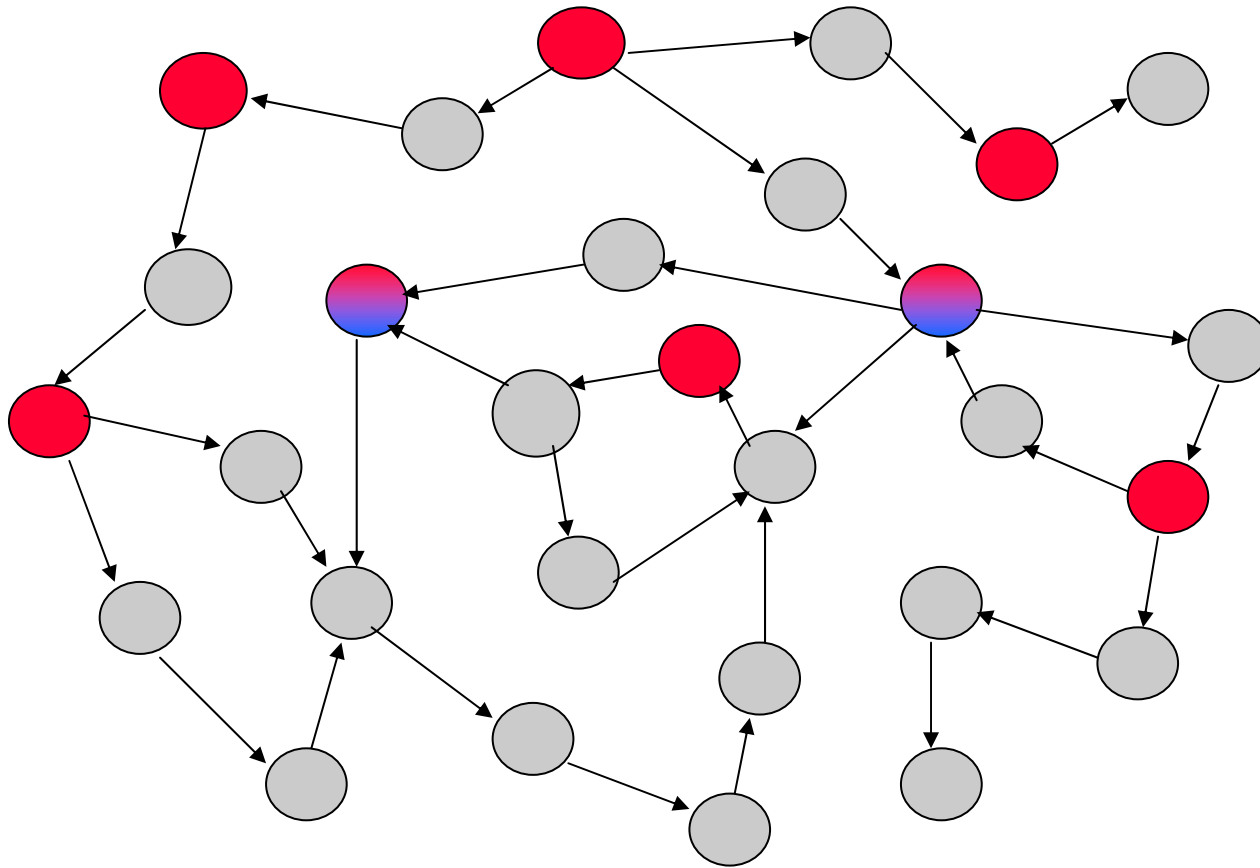


# BFS With Snapshots (period=2)





# Duplicates Detected!



# BFS with Snapshots

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## Algorithm 2 BFS with Snapshots

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**Require:** Sampling function  $f : \mathbb{N} \rightarrow \mathbb{B}$ , number of snapshots  $n$

**procedure** BFSWS( $s_0$ )

$i, j \leftarrow 0, Open \leftarrow \{s_0\}, S_0, \dots, S_{n-1} \leftarrow \emptyset$  {Initial state added to horizon}

$S_j \leftarrow Open$  {First snapshot contains initial state}

**while**  $Open \neq \emptyset$  **do** {Repeat until there are no more states to explore}

$i \leftarrow i + 1, Next \leftarrow \emptyset$  {The next level ( $i + 1$ ) is currently empty}

**for all**  $s \in Open$  **do** {Explore all states in the horizon}

$Next \leftarrow Next \cup \{s' \mid \exists \ell. (s, \ell, s') \in en(s)\}$

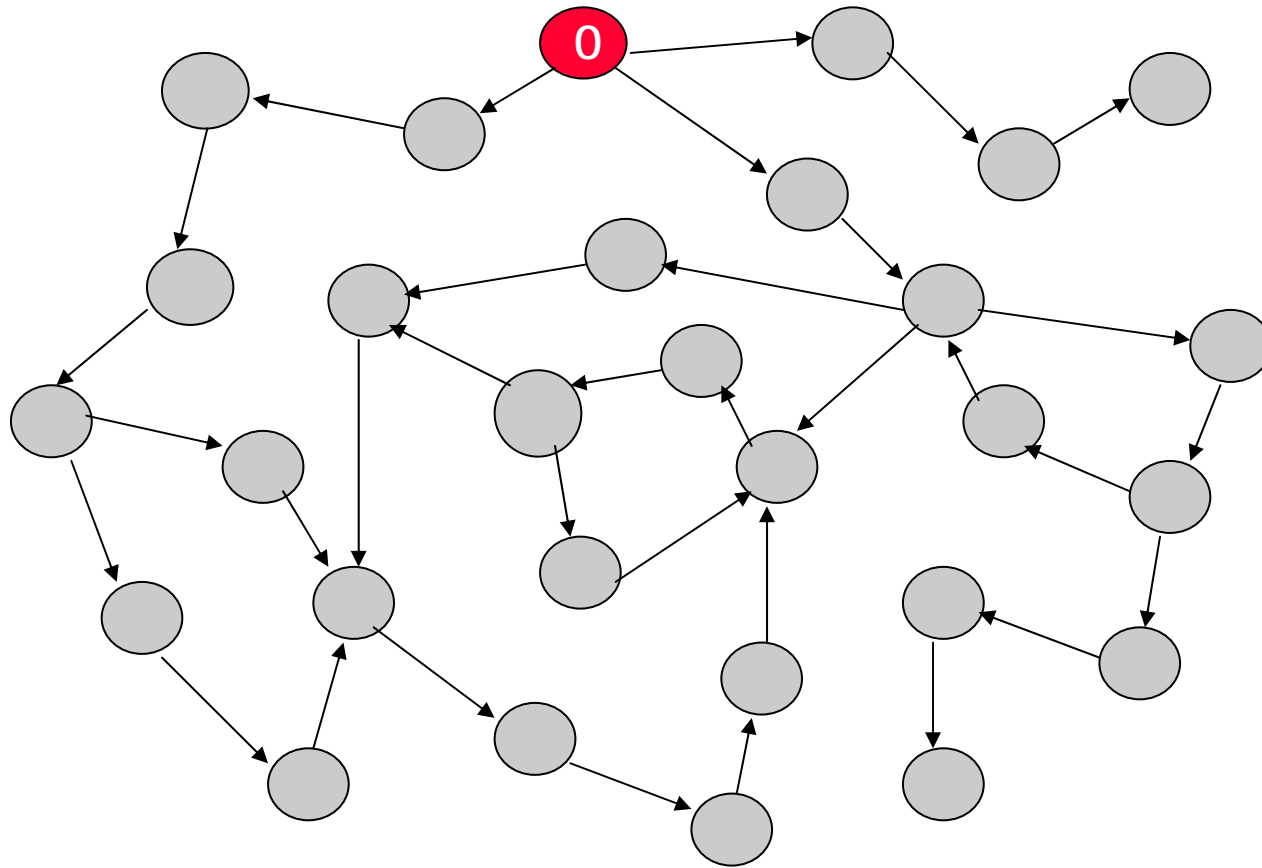
$Open \leftarrow Next \setminus \bigcup_{k=0}^{n-1} S_k$  {Add new states to horizon}

**if**  $f(i)$  **then**  $j \leftarrow j + 1 \bmod n, S_j \leftarrow Next$  {Should this level be sampled?}

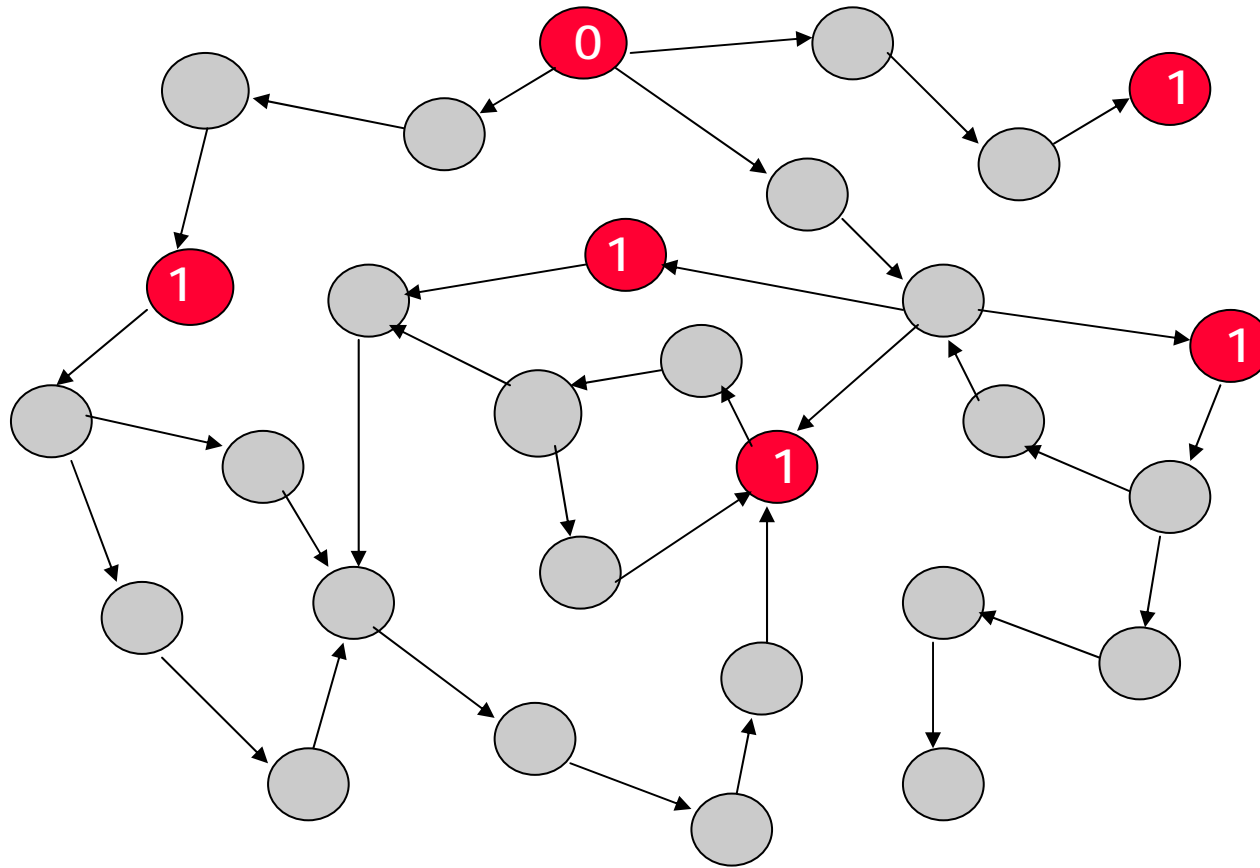
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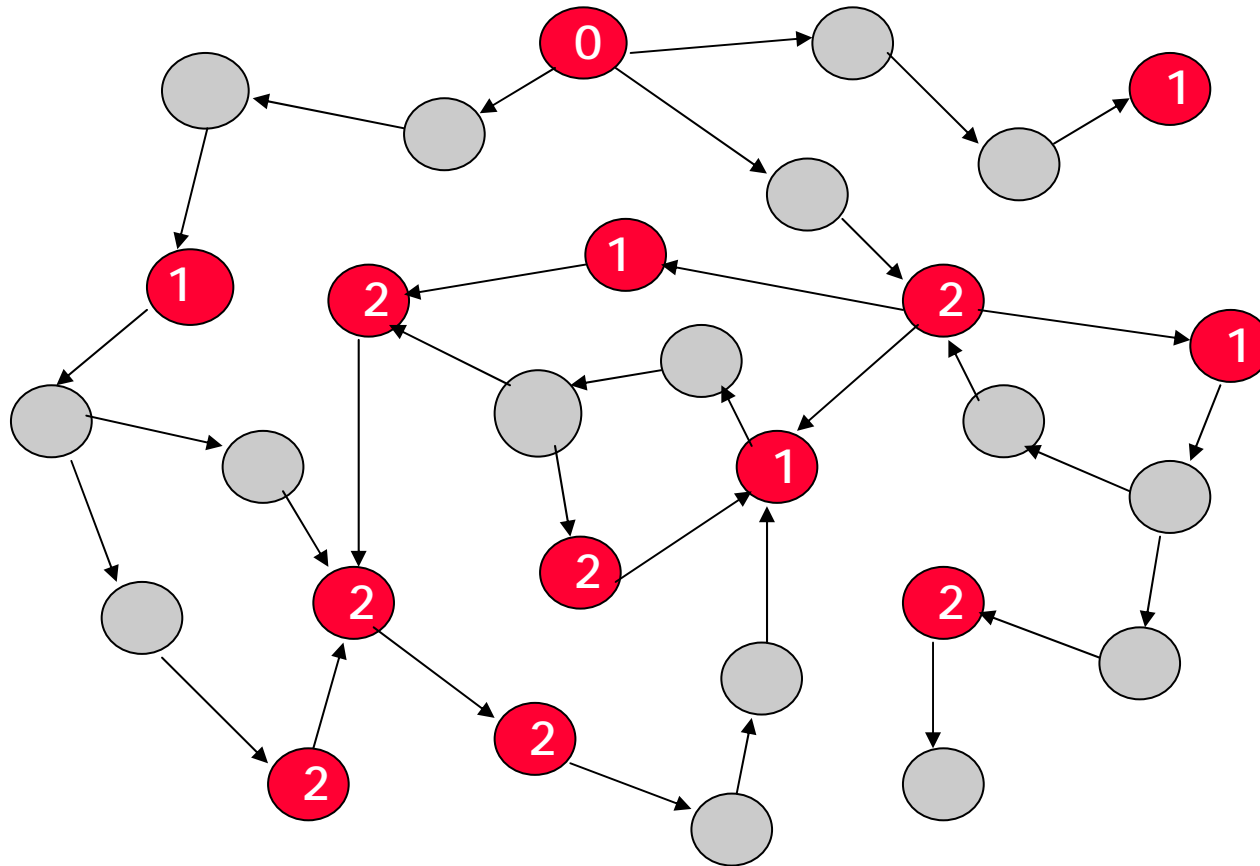
# BFS With Snapshots (period=3)



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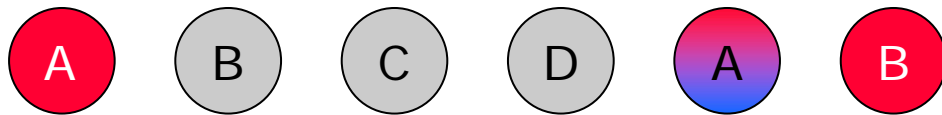
# BFS With Snapshots (period=3)



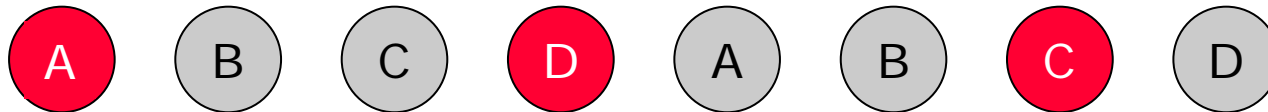


# BFS With Snapshots

- With  $n=1$ , if sampling period  $\geq$  size of cycle, then detect



- NO detect if sampling period  $<$  size of cycle!



- Let sampling period increase along search, then termination!



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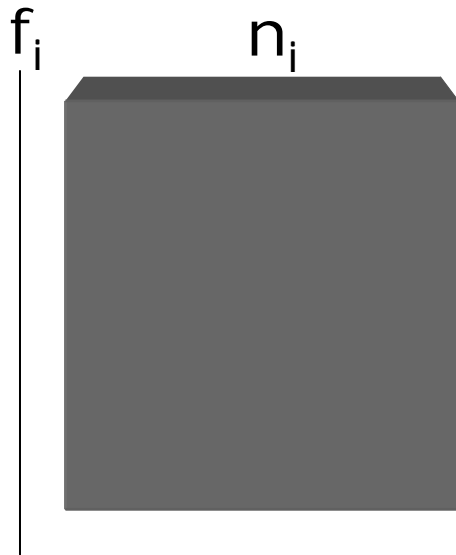
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# BFS With Snapshot Caches

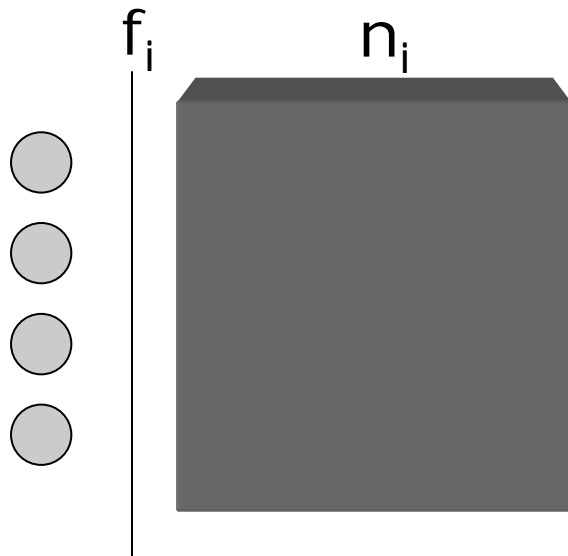
- Similar to
  - Fast memory cache for CPU
  - Cache of web browsers
- Selectively store history in memory
  - Usually, to speed up process
  - For LTSs, to reduce memory use



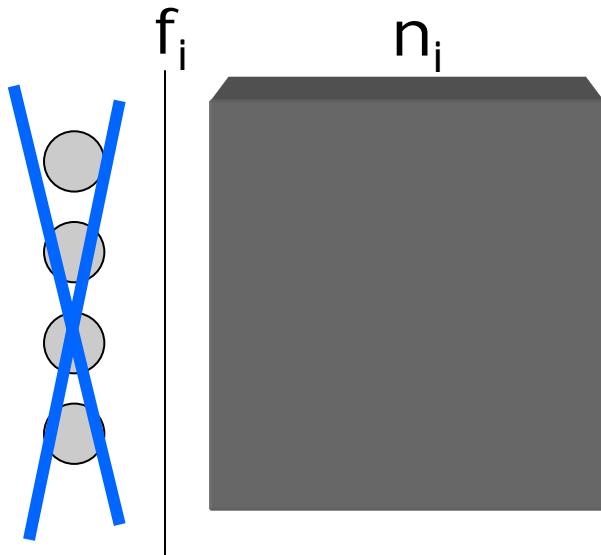
# BFS With Snapshot Caches



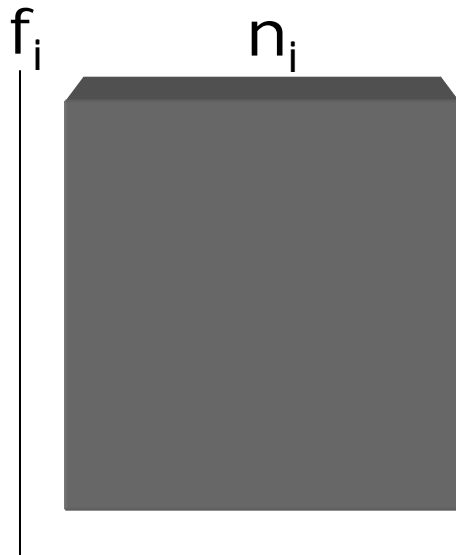
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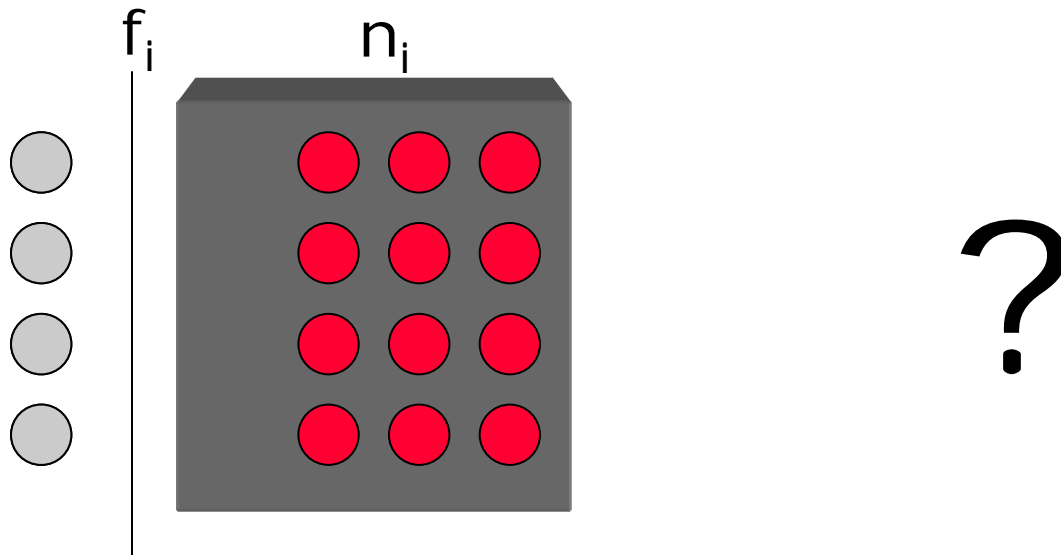
# BFS With Snapshot Caches



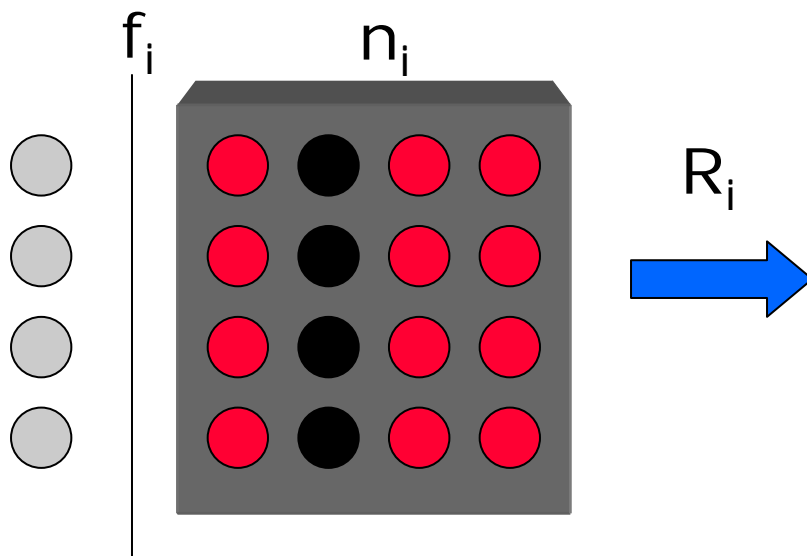
# BFS With Snapshot Caches



# BFS With Snapshot Caches



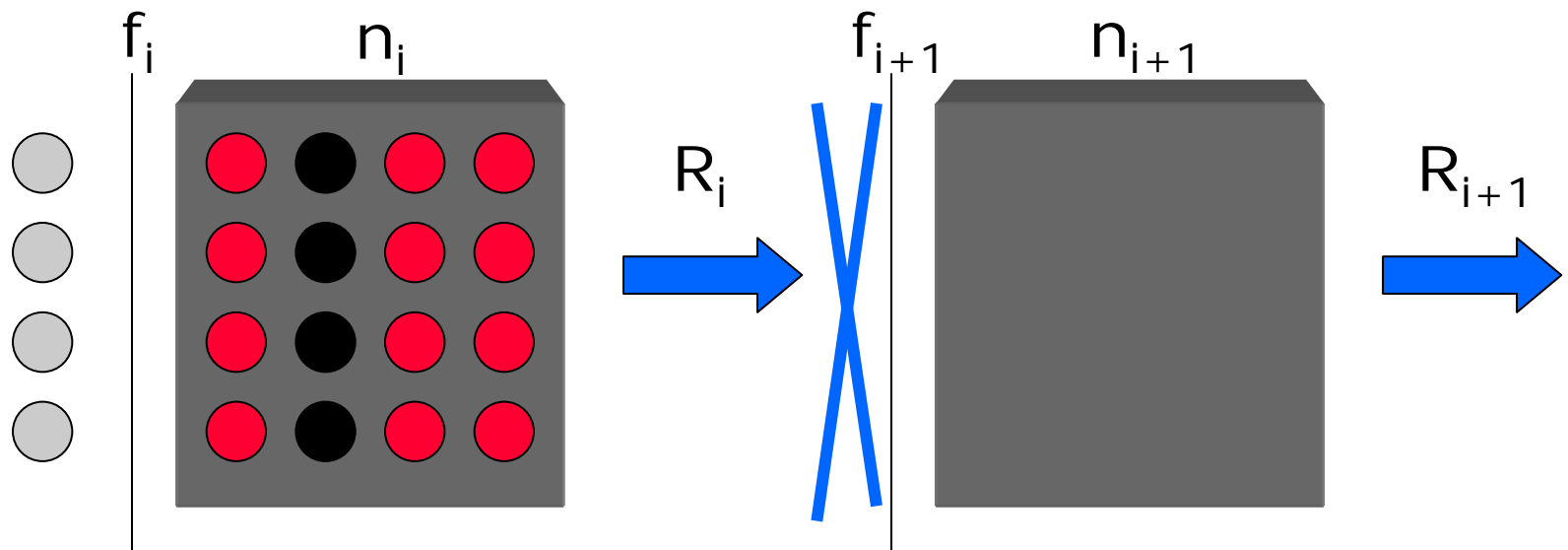
# BFS With Snapshot Caches



- Least recently used
- Most recently used
- Least frequently used
- Most frequently used
- Snapshot size
- Level number (FIFO)
- Random



# BFS With Snapshot Caches





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# Implementation

- General Machinery in CADP
- Cache library allows creation of hierarchies of caches, each storing finite number of elements, each element paired with meta-information
- Predefined/user-specified replacement strategies
- DFS: states / BFS: levels, uniquely stored (counters)



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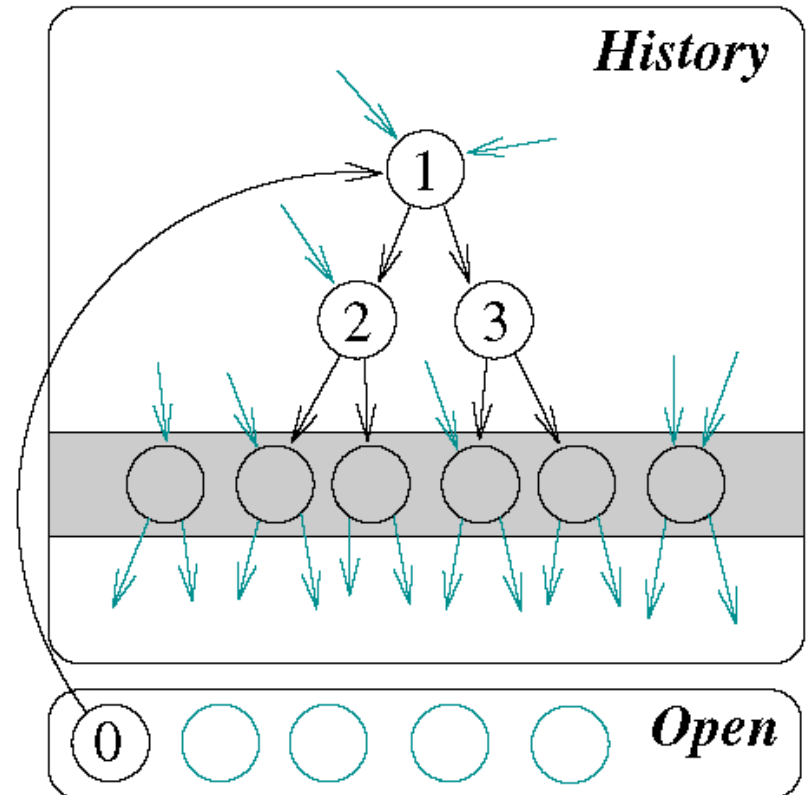
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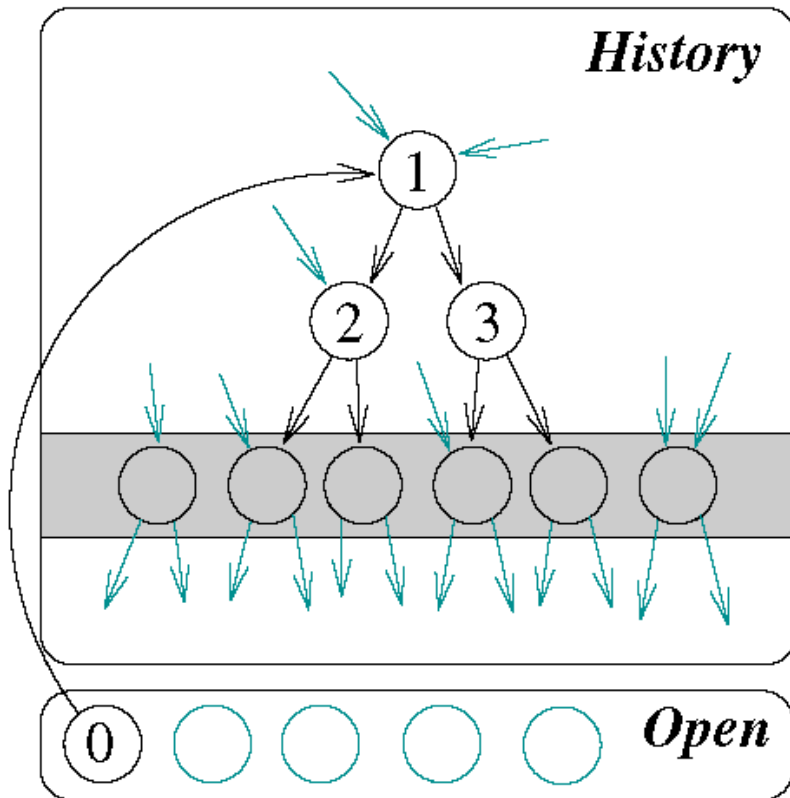


# Frontier Safety Net

- Earlier attempts use *locality l*; maximum jump back in search
- *Frontier Search* (Korf et al. 2005) stores last *l* levels
- Hash table with replacements (Tronci et al. 2001)
- -> Useful when *l* small (protocols)
- We can generalise, by using two caches, first FIFO frontier (period constant), second safety net (increasing period)



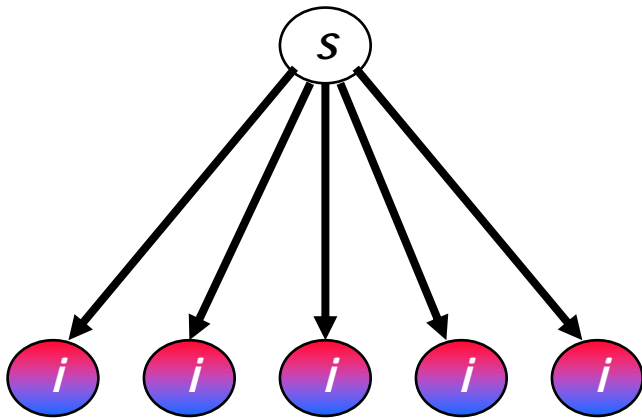
# Adaptive: Backtracking



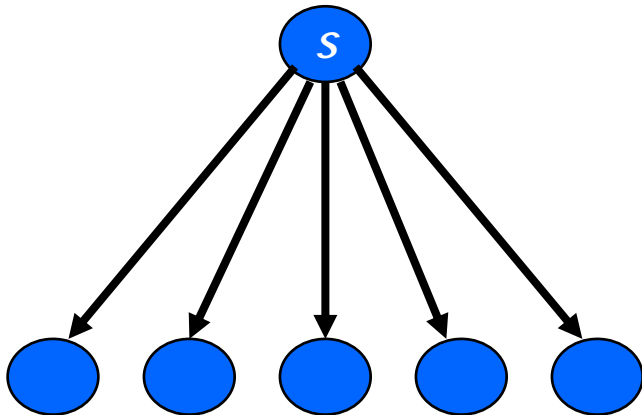
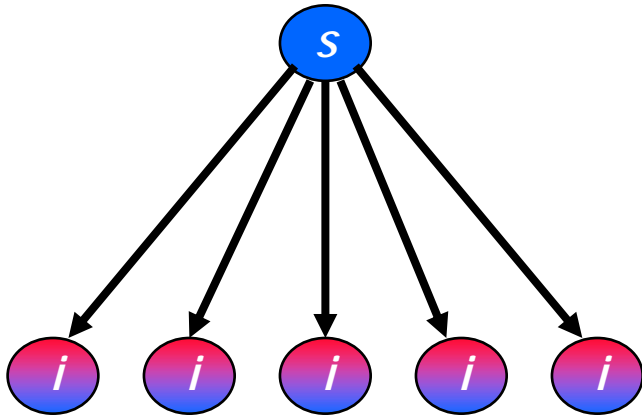
- Detection failure leads to  $\sum_{i=1..d} b^i$  extra traversals, with  $b$  branching factor,  $d$  distance to next snapshot

# Adaptive: Backtracking

- Observation: if all  $n$  successors of  $s$  appear in a single snapshot  $i$ , perhaps  $s$  explored before ( $n > 1$ )



# Adaptive: Backtracking

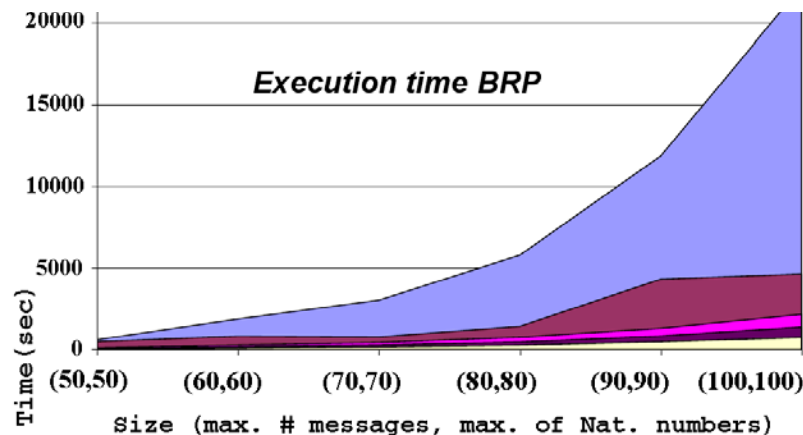
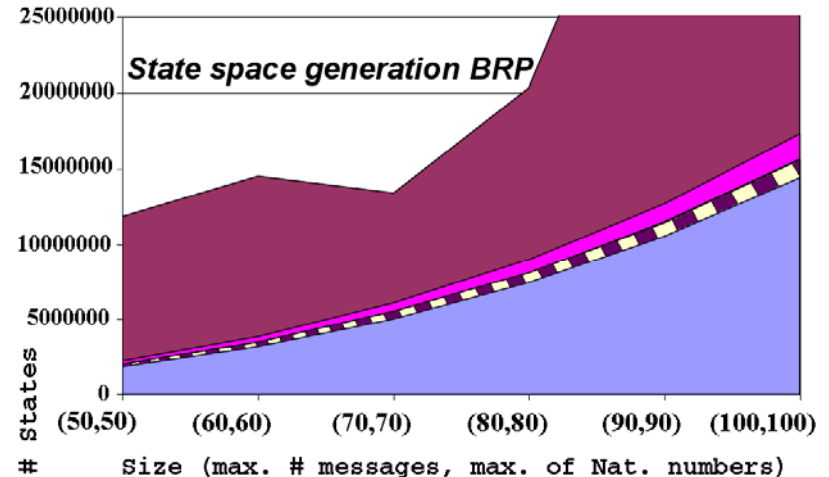
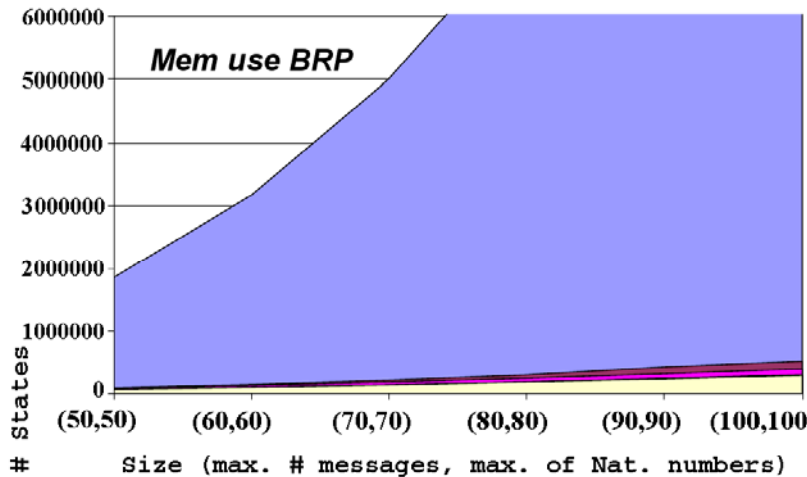


- -> Put  $s$  in special set of states if all succs
  - Either in 'old' snapshot  $i$ 
    - In stream of caches  $C_1$ - $C_2$ ...,  $n$  in  $C_i$ ,  $i > 1$
  - Or in special set
- This set also used for duplicate detection



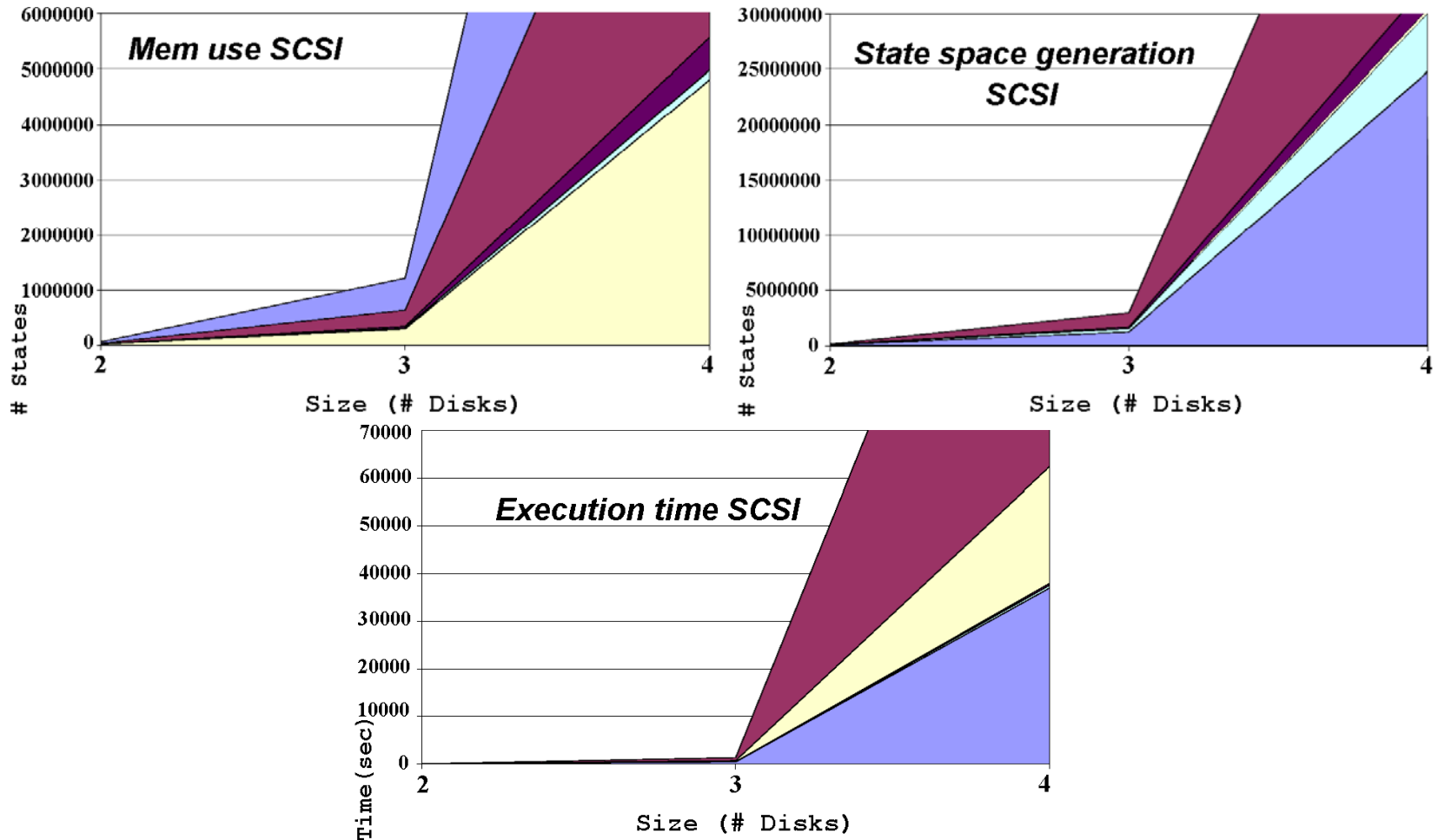
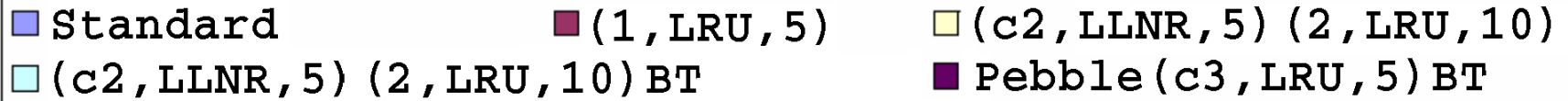
# Experimental Results

■ Standard     
 ■ (1, LFU, 5)     
 ■ (c2, LLNR, 5) (2, LFU, 10)  
■ Pebble (c3, LRU, 5)     
 ■ (c2, LLNR, 5) (2, LFU, 10) BT

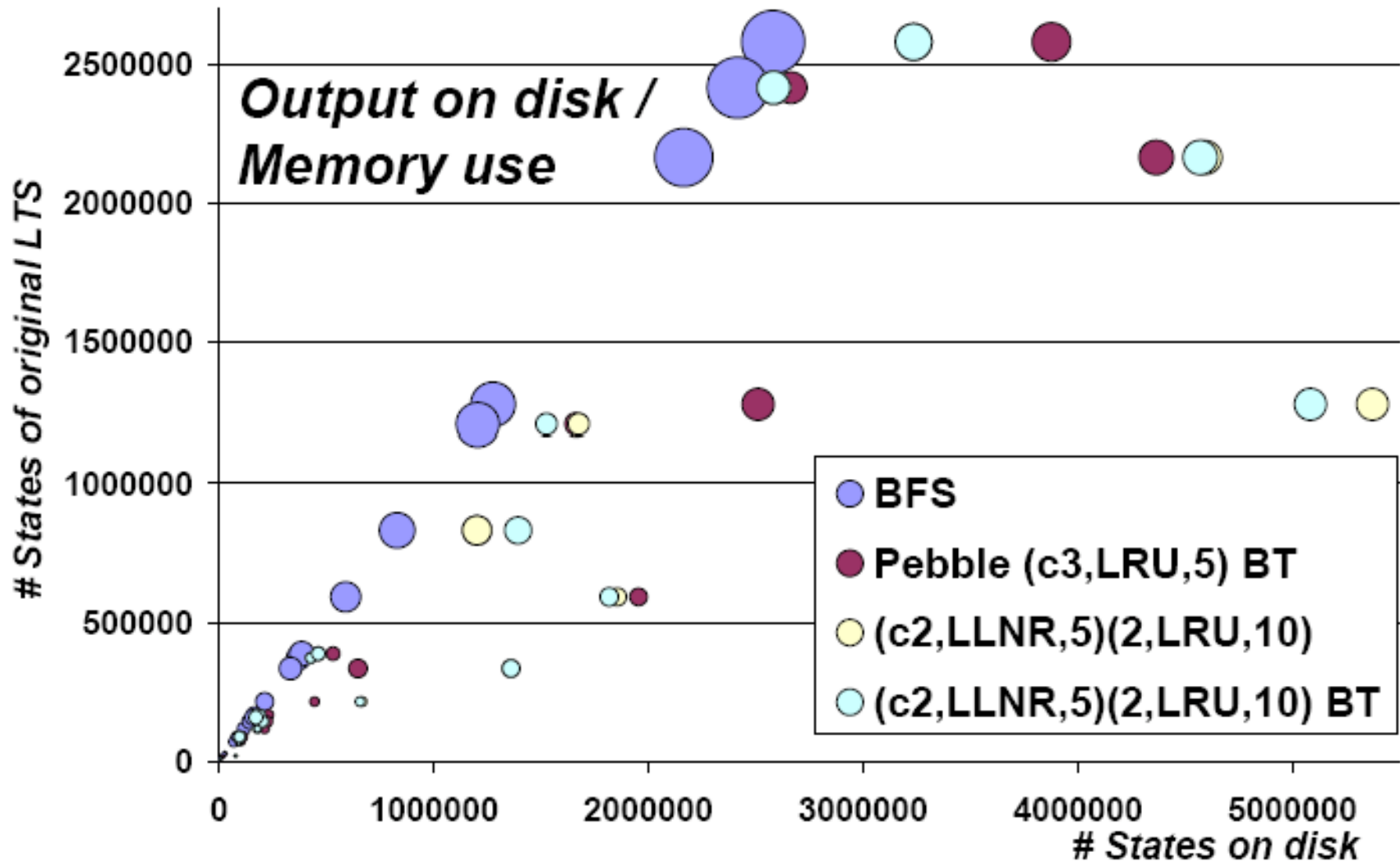




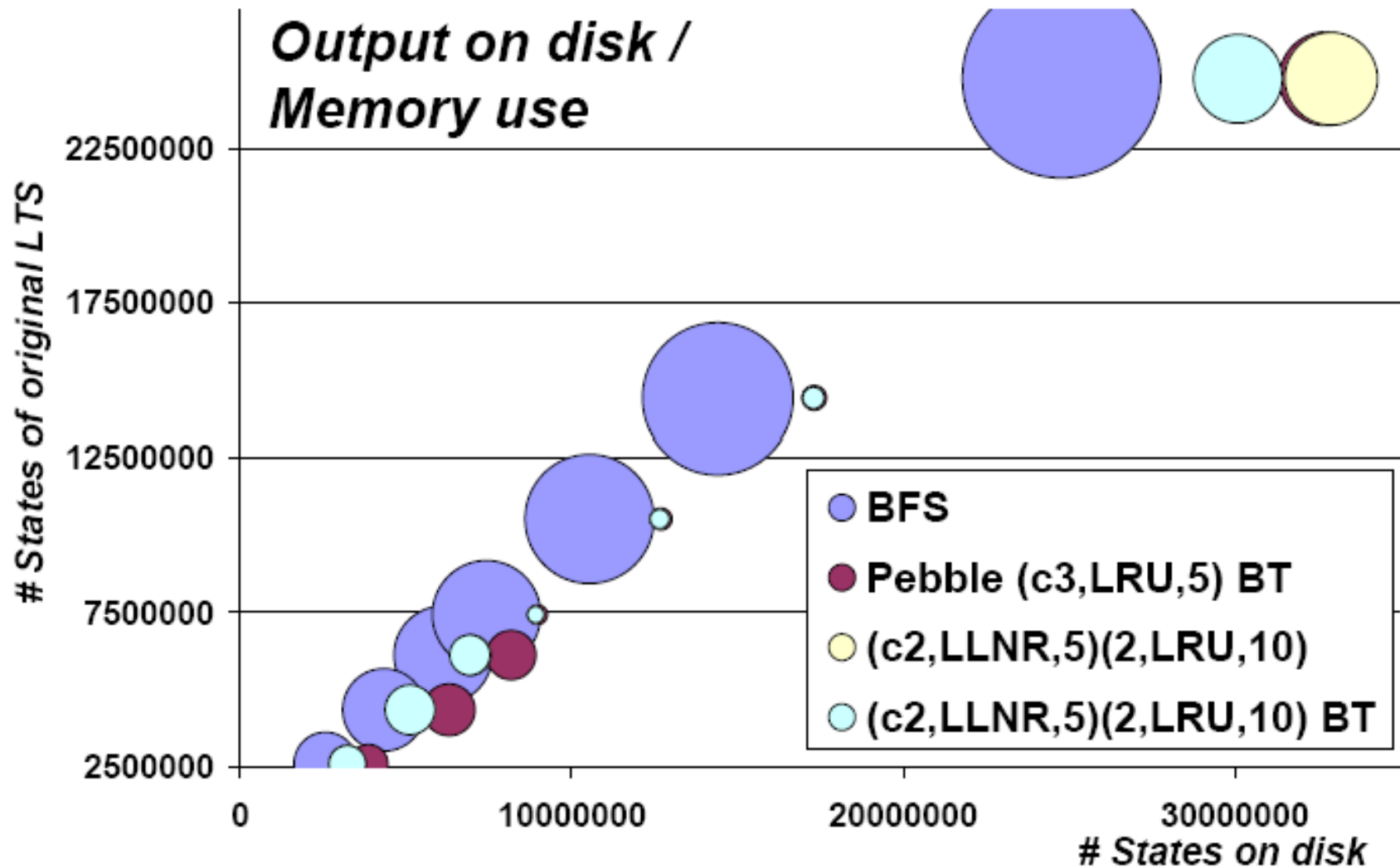
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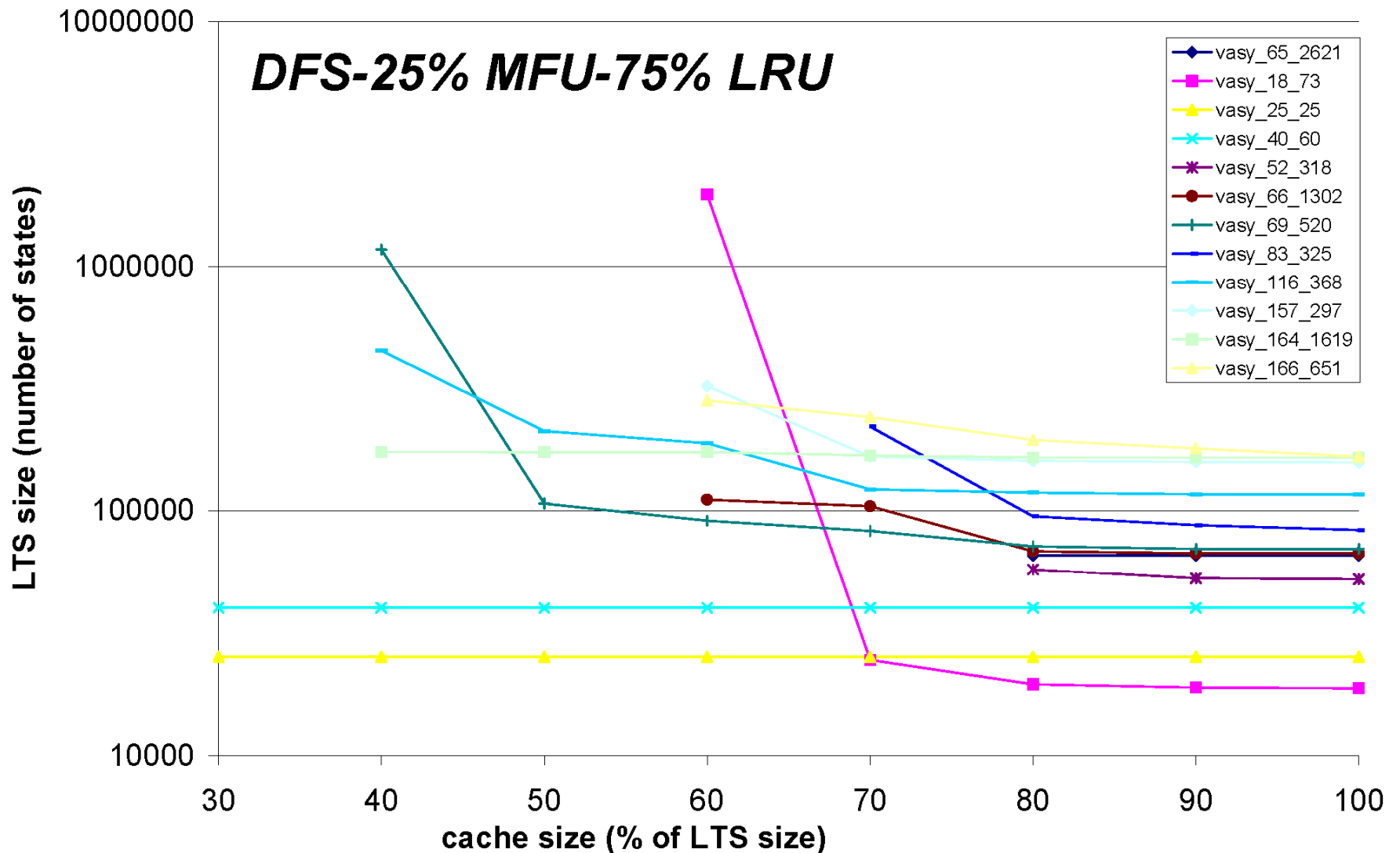


# Depth-first Search

- States in Memory
  - Stack used to store current trace
  - Caches store additional individual states
- Best strategies, size LTS < twice original
  - LRU (up to 40% reduction)
  - MFU
  - Random
- Comparable to results of Holzmann '87
- Combination of two caches <MFU,LRU> and <RND,LRU> with LRU 25% of size, up to 30% reduction
- Overall best performance: <MFU,LRU> and <RND,LRU> with LRU 75% of size



# Depth-first Search



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# Conclusions

- Delivered general machinery for hierarchical, adaptive state space caching in CADP
- The techniques are
  - Alternatives to existing methods
  - Concerned with generation
  - Guaranteeing exhaustiveness and termination
  - Useful for general LTSs
- Backtracking is an adaptive mechanism which either has a positive effect or hardly an effect -> can be used by default
- Effectiveness DFS with caching differs more from one case to the other
  - 'fixed size' cache hard to determine a priori
  - BFS with caching simply takes as much memory as needed



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# Future Work

- More experiments
  - Find other adaptive sampling mechanisms
  - Develop more robust setups
- Use for
  - Distributed state space generation
  - On-the-fly state space reduction





# No guarantee exhaustiveness

- When hashes (positions in *Closed* list) of states collide:
  - Assume new state already visited
    - Holzmann '87, '88
    - Courcoubetis et al. '92
  - Always replace old state -> loss of termination
    - Tronci et al. 2001
- Probabilistic BFS
  - Tronci et al. 2001
- Stern & Dill '96 reduce prob. of failure



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# Pebble Search

- As throwing a pebble in a pool, creating waves which die out
- Creates new cache when old ones are full, due to sampling functions taking longer to be filled
- -> Rippling effect
- Use constant sampling functions
- Generalisation of Frontier Search

